

POST-QUANTUM CRYPTO: CHALLENGES FOR EMBEDDED APPLICATIONS

Joppe Bos
APRIL 2022



SECURE CONNECTIONS
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POST-QUANTUM CRYPTO FOR EMBEDDED DEVICES?

Outline

- Risk assessment: when to act?

Embedded perspective

- PQC performance
- High-assurance implementations

HOW TO PREPARE FOR HURRICANE SEASON Quantum



MAKE A PLAN

Amren should create an emergency plan and/or checklist:

- obtain supplies
- update personal documents
- secure household
- research evacuation options/routes
- update prescriptions



CREATE A GO-BAG

Prepare supplies ahead of a hurricane. These can include:

- Food/water
- Additional clothes
- Personal documents
- Travel supplies
- Prescriptions



KNOW YOUR WING GUIDANCE

Whether preparing for a hurricane or evacuating, know your wing or installation's guidance. Routinely check for updates from leadership and maintain communication with your chain of command.



RECOGNIZE WARNINGS & ALERTS

Have several ways to receive alerts. Download real-time alert apps. Sign up for community alerts in your area and be aware of the Emergency Alert System (EAS) and Wireless Emergency Alert (WEA), which requires no sign up.



STAY SAFE

Practice good hygiene and safety measures during any part of a hurricane evacuation or impact. Keep family considerations in mind and don't be afraid to contact leadership for guidance.

QUANTUM COMPUTERS - PROGRESS

VOLUME 80, NUMBER 15 PHYSICAL REVIEW LETTERS 13 APRIL 1998

Experimental Implementation of Fast Quantum Searching

Isaac L. Chuang,^{1,*} Neil Gershenfeld,² and Mark Kubinec³

¹IBM Almaden Research Center K10/D1, 650 Harry Road, San Jose, California 95120

²Physics and Media Group, MIT Media Lab, Cambridge, Massachusetts 02139

³College of Chemistry, D7 Latimer Hall, University of California, Berkeley, Berkeley, California 94720-1460

(Received 21 November 1997; revised manuscript received 29 January 1998)

WIRED BACKCHANNEL BUSINESS CULTURE GEAR LEGALS SCIENCE SECURITY

TOM SIMONETT BUSINESS 12.03.2020 02:00 PM

China Stakes Its Claim to Quantum Supremacy

Google trumpeted its quantum computer that outperformed a conventional supercomputer. A Chinese group says it's done the same, with different technology.

1998:
2 qubit

2018:
72 qubit

2020: Quantum
Supremacy #2

2006: 1
2 qubit

2019:
Quantum
Supremacy
#1

2021:
127 qubit

Google AI Blog

The latest from Google Research

Quantum Supremacy Using a Programmable Superconducting Processor

Wednesday, October 23, 2019

IBM Unveils Breakthrough 127-Qubit Quantum Processor

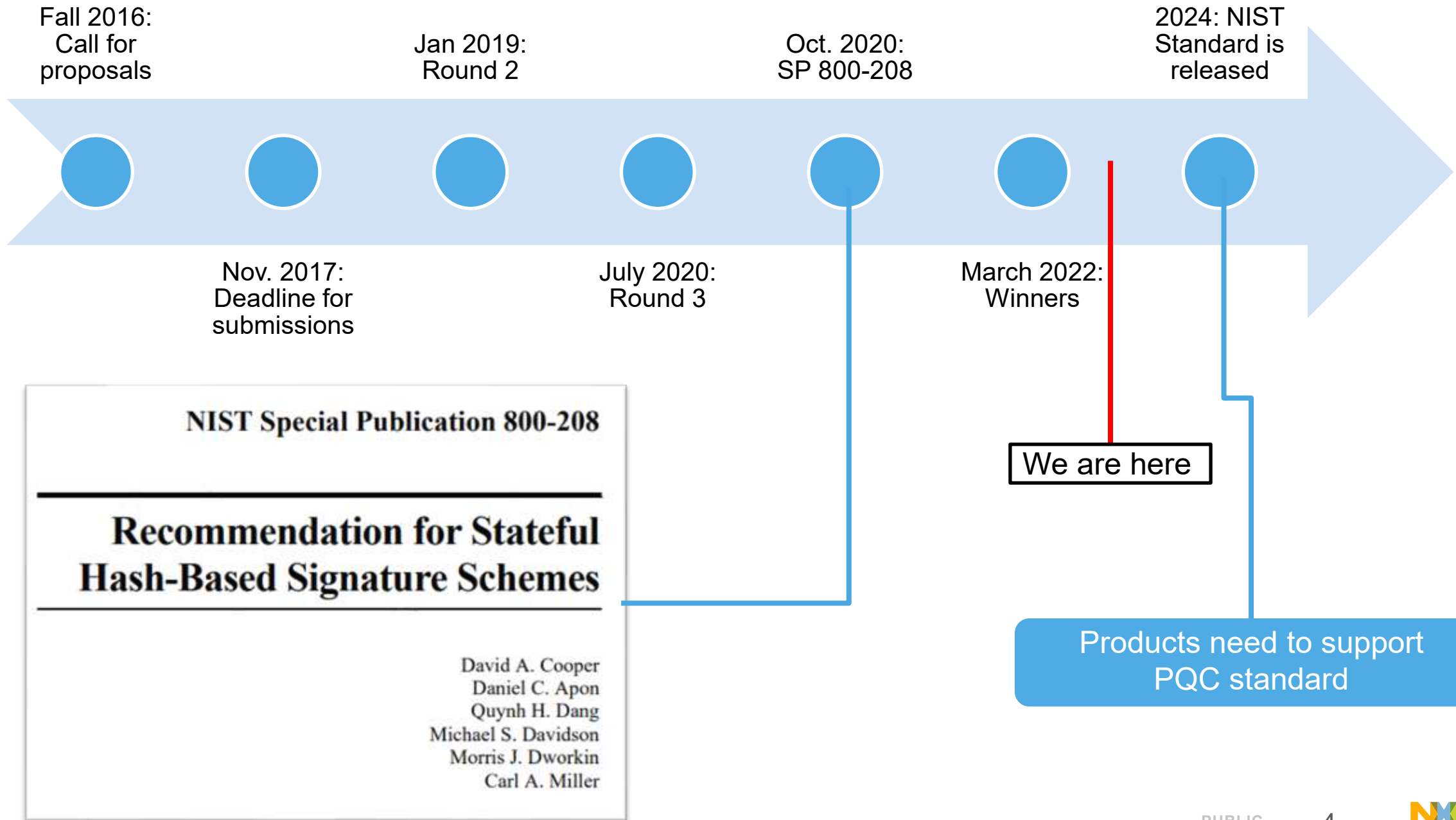
- Delivers 127 qubits on a single IBM quantum processor for the first time with breakthrough packaging technology
- New processor furthers IBM's industry-leading roadmaps for advancing the performance of its quantum systems
- Previews design for IBM Quantum System Two, a next generation quantum system to house future quantum processors

Nov 16, 2021



**POST-QUANTUM CRYPTO STANDARDS ARE COMING
IT DOESN'T MATTER IF YOU BELIEVE IN QUANTUM COMPUTERS OR NOT**

POST-QUANTUM CRYPTO STANDARDS TIMELINE



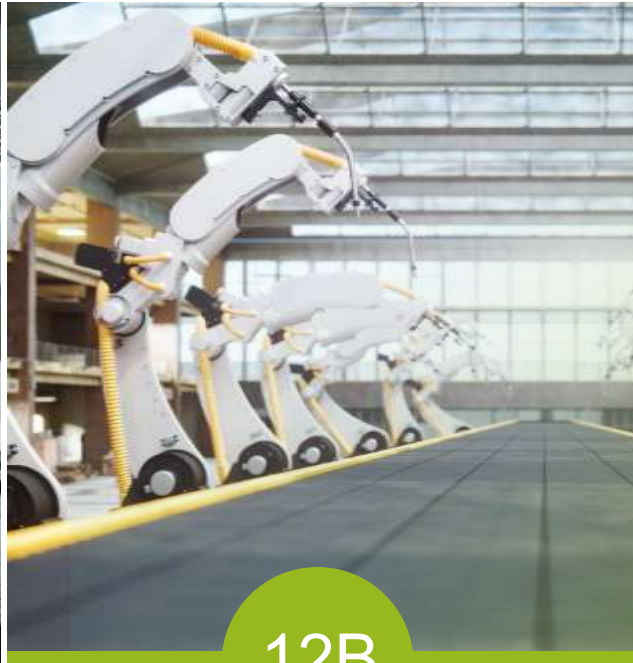
POST-QUANTUM CRYPTO IS ON THE HORIZON

AUTOMOTIVE



70% connected cars by 2025

INDUSTRIAL & IOT



IoT Edge & end nodes from **6B units** in 2021 to **12B units** in 2025

MOBILE



Tagging **60B products** per year by 2025

COMMUNICATION INFRASTRUCTURE



Secure anchors & services for **40B processors**

What is the impact on the billions of embedded devices?



TYPICAL EXAMPLES

Automotive

New platform designed now will likely enter the market after 2024 and remain in use for many years

(Industrial) IoT

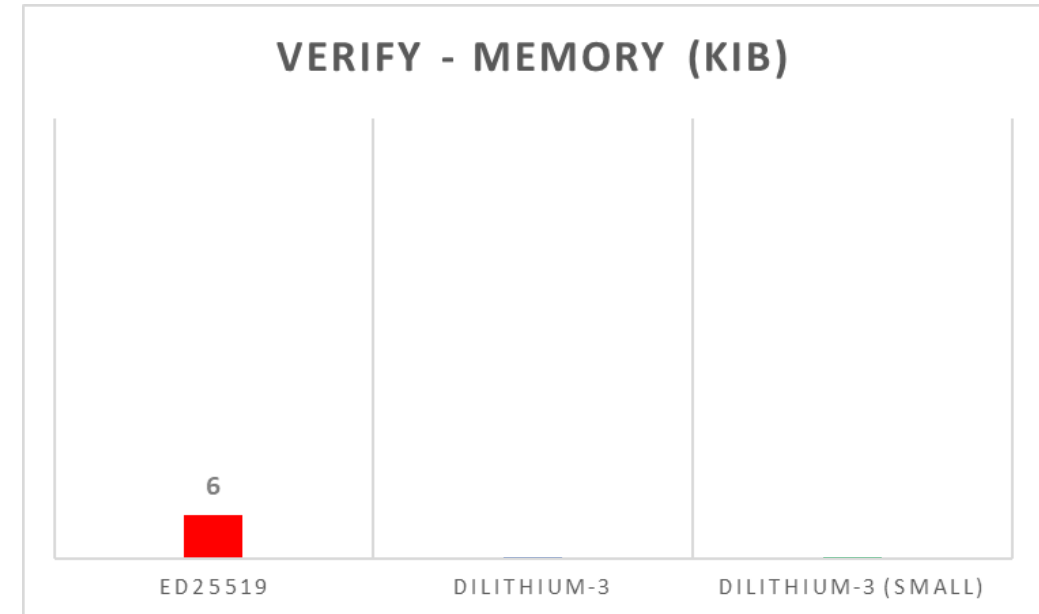
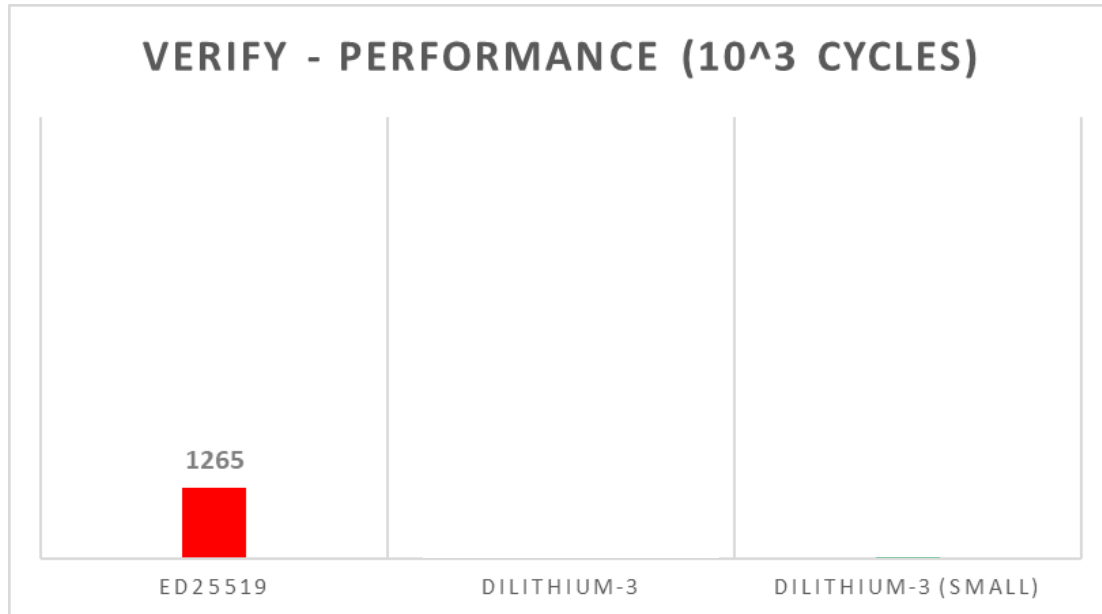
Devices sold now need to be able to support the new PQC standard in 2024: crypto agility

Many embedded IoT platforms are resource constrained:
4-16 KiB memory



SIGNATURE VERIFICATION – ECC VERSUS PQC

Academic figures on ARM Cortex-M4



Typical crypto operation: signature verification

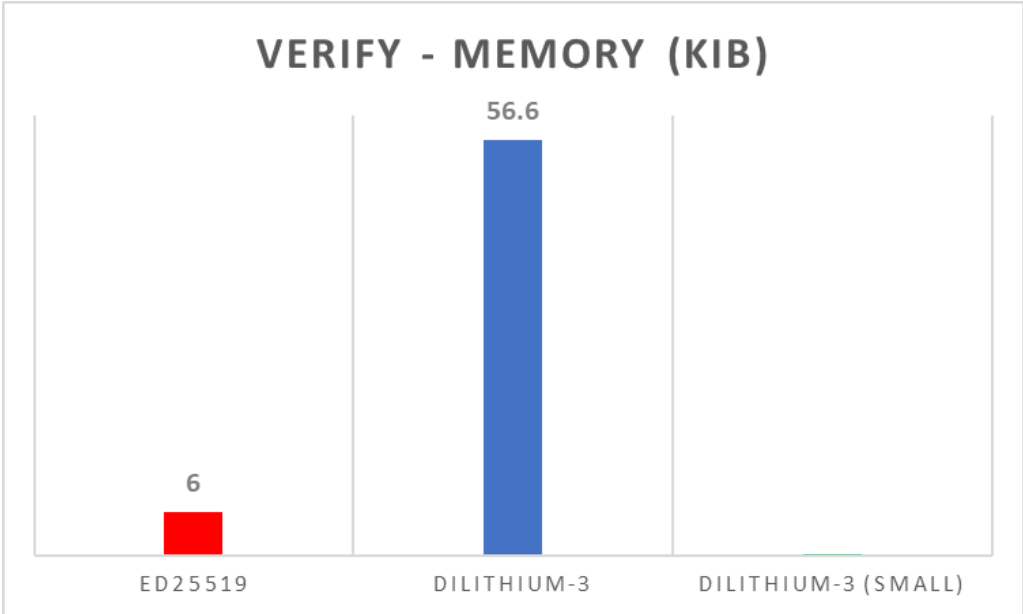
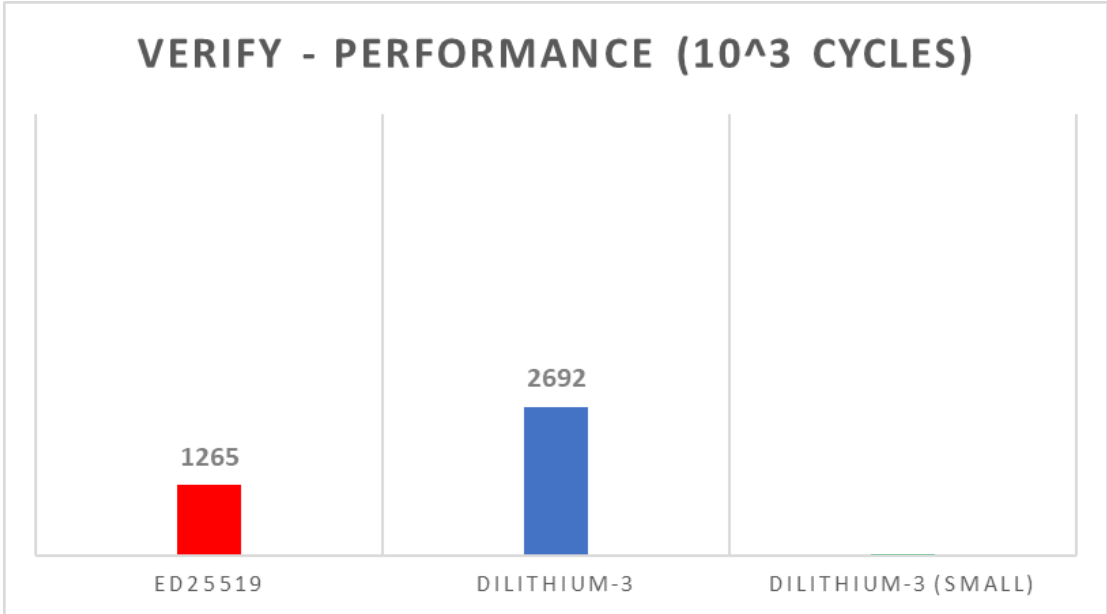
- Secure boot
- Secure (over-the-air) update

Size (bytes)	Ed25519	Dilithium-3
Private key	64	4000
Public key	32	1952
Signature	64	3293

- Ed25519 numbers from Fujii, Aranha. Curve25519 for the Cortex-M4 and beyond. In LatinCrypt 2017

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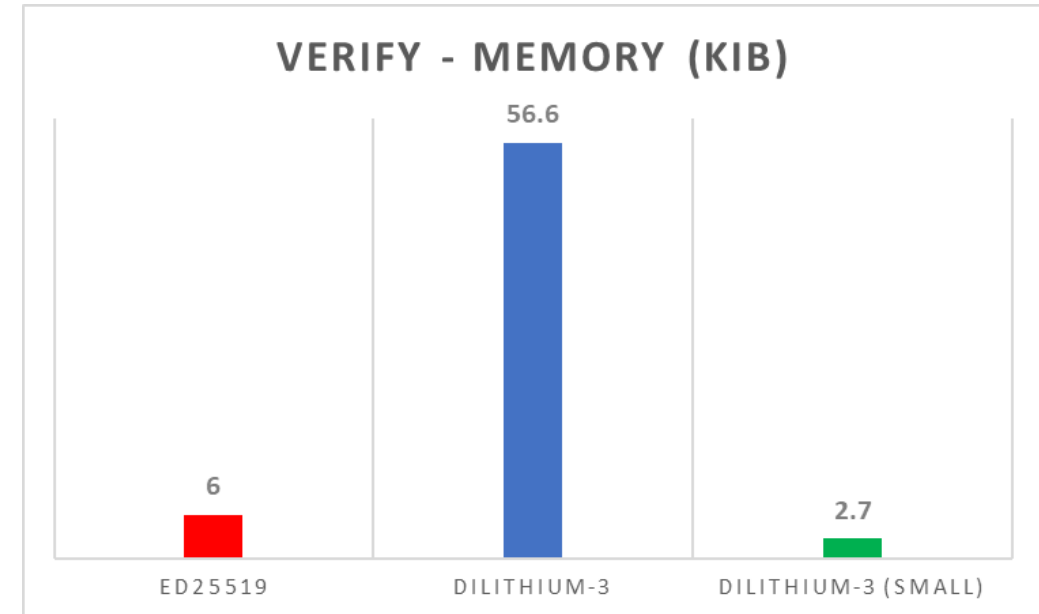
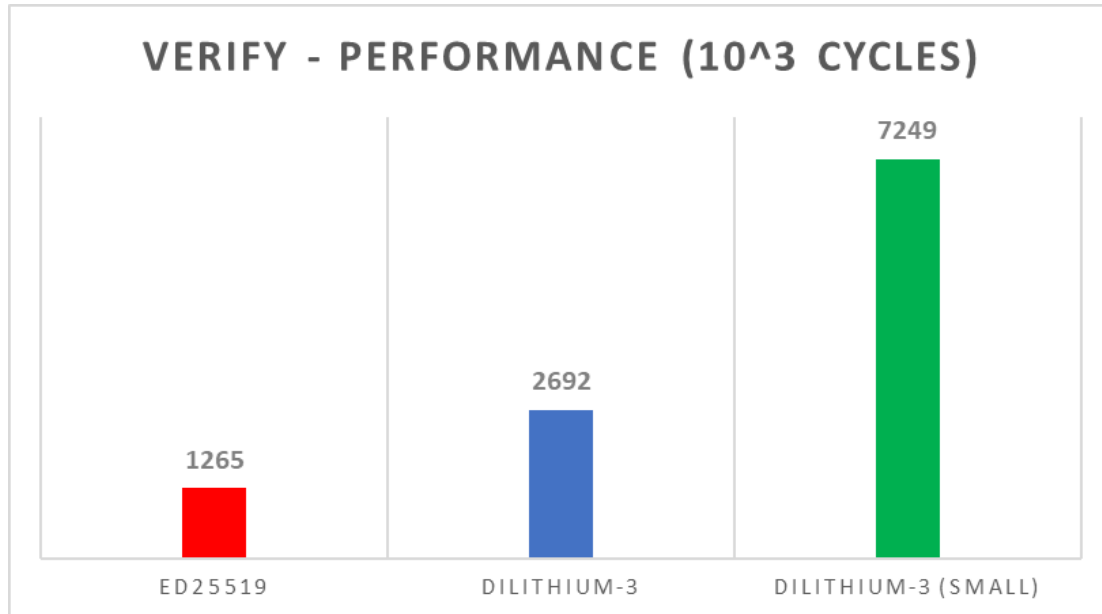
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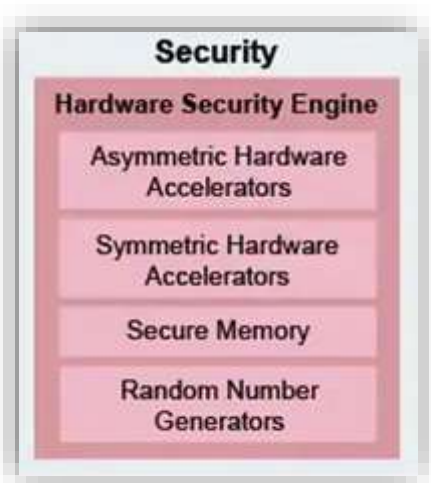
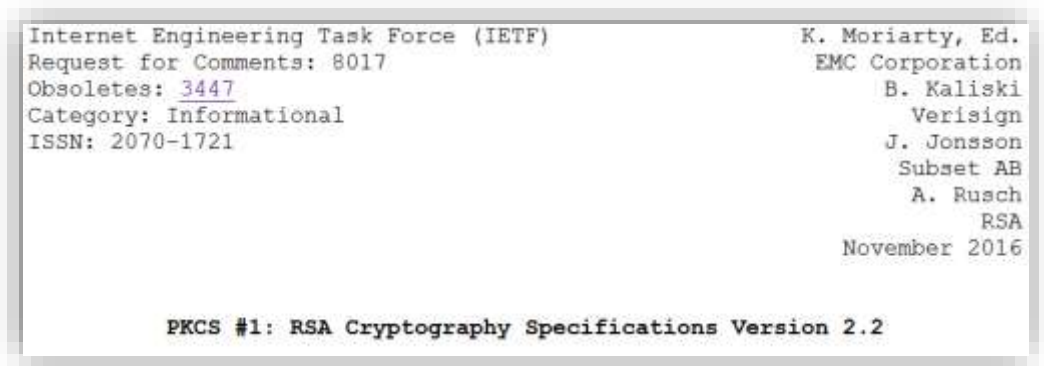
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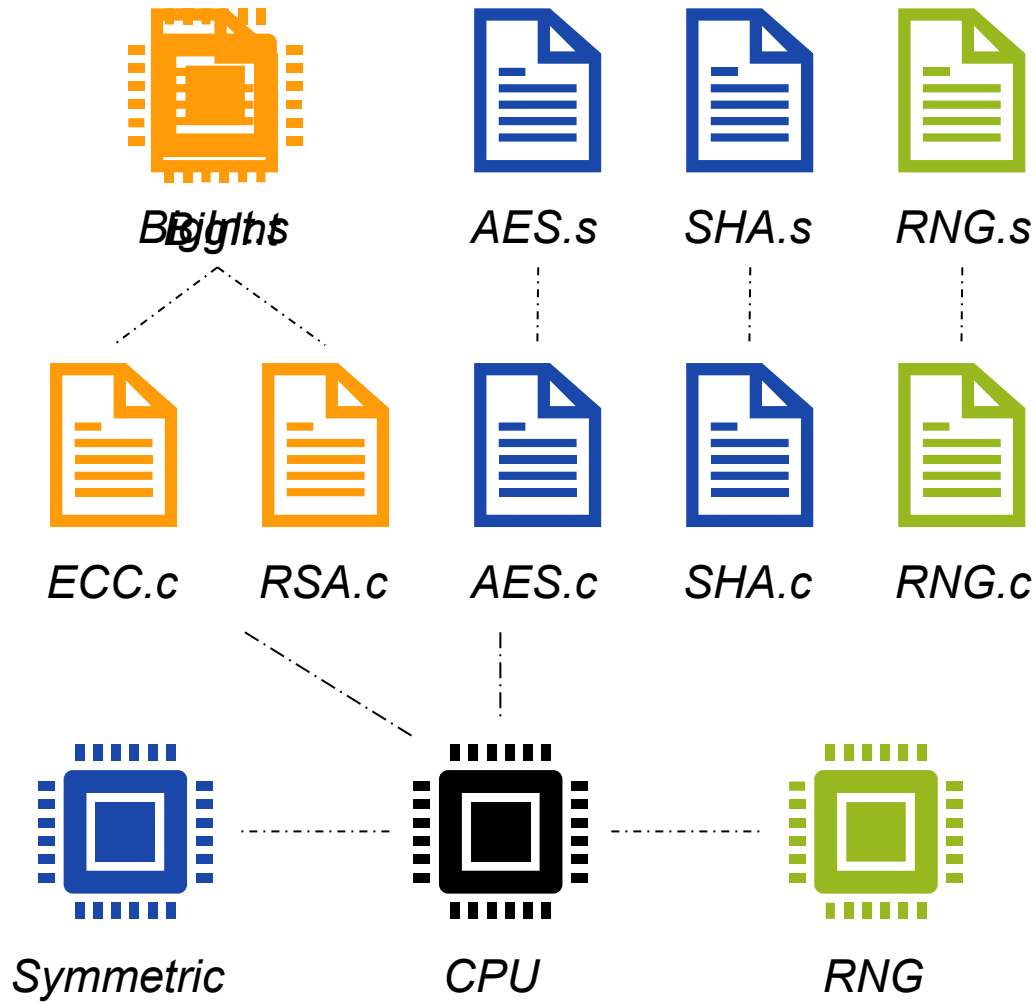
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- **Bos**, Renes, Sprenkels: Dilithium for Memory Constrained Devices. Cryptology ePrint Archive, Report 2022/323

IMPLEMENTING CLASSICAL CRYPTOGRAPHY



S32G2 automotive processor spec



1. <https://www.nxp.com/products/processors-and-microcontrollers/arm-processors/s32g-vehicle-network-processors:S32G-PROCESSORS>

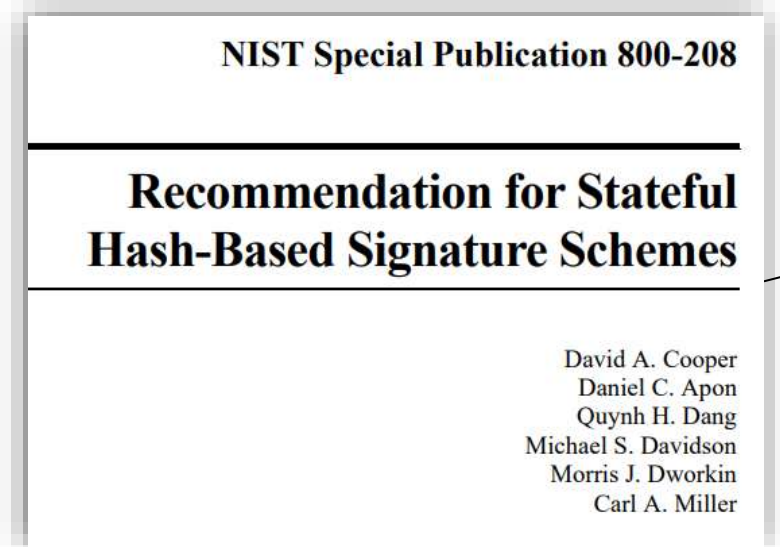
IMPLEMENTING POST-QUANTUM CRYPTOGRAPHY



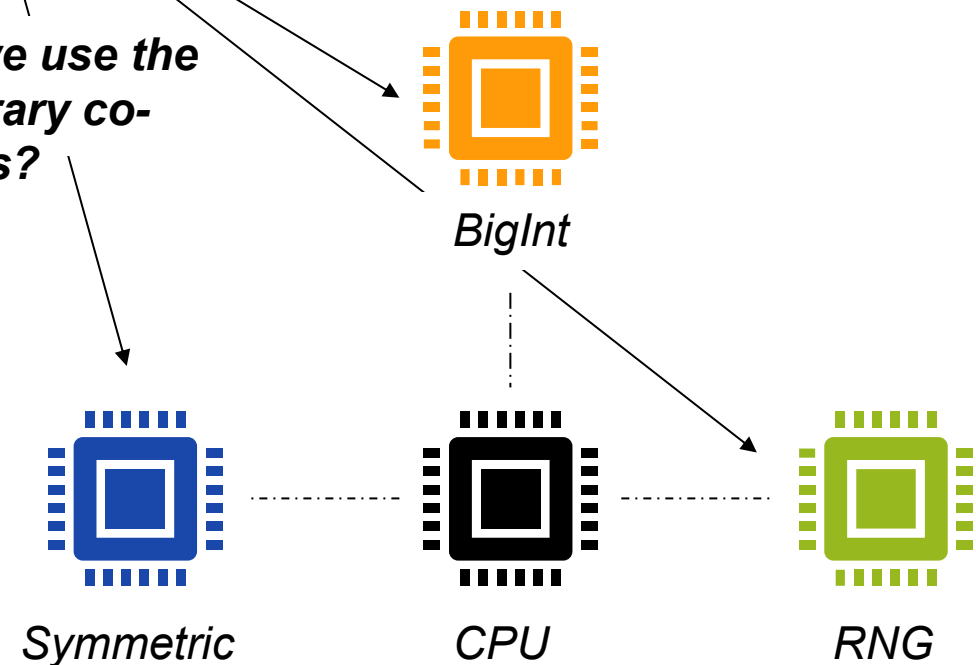
- ▶ For the lattice KEMs, the main decision will be Kyber/NTRU/Saber
- ▶ Similarly for lattice signatures, the main decision will be Dilithium/Falcon

-- Dustin Moody (NIST R3 Status Update)

How can we use the contemporary co-processors?



XMSS
LMS



REUSING EXISTING COPROCESSORS



Approach	Core	Structure	Size
RSA	Modular multiplication	$(\mathbb{Z}/n\mathbb{Z})^*$	n is 3072-bit
ECC	Elliptic curve scalar multiplication	$E(\mathbb{F}_p)$	p is 256-bit
Lattice	Polynomial multiplication	$(\mathbb{Z}/q\mathbb{Z})[X]/(X^n + 1)$	q is 16-bit n is 256

Lattice cryptography uses 16-bit coefficients, how to use our bignum coprocessors?

Proposal from [A] for 128-bit coprocessors

Pack multiple 16-bit coefficients in large 128-bit register

Ensure sufficient “space” is reserved to avoid overflow

[A] Albrecht, Hanser, Hoeller, Pöppelmann, Virdia, Wallner: Implementing RLWE-based schemes using an RSA co-processor. TCHES 2019

KRONECKER SUBSTITUTION: POLYNOMIAL MULTIPLICATION WITH INTEGER MULTIPLIERS

Polynomial domain

$$f = 1 + 2x + 3x^2 + 4x^3$$

$$g = 5 + 6x + 7x^2 + 8x^3$$

✖

$$fg = \underline{5} + \underline{16x} + \underline{34x^2} + \underline{60x^3} + \underline{61x^4} + \underline{52x^5} + \underline{32x^6}$$

Kronecker domain (with evaluation point 100)

$$f(100) = 4030201$$

$$g(100) = 8070605$$

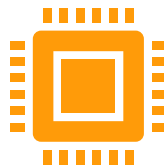
✖

$$fg(100) = \underline{32526160341605}$$

Grundzüge einer arithmetischen Theorie der
algebraischen Grössen.

(Von L. Kronecker.)

(Abdruck einer Festschrift zu Herrn E. E. Kummers Doctor-Jubiläum, 10. September 1881.)



REUSING EXISTING COPROCESSORS



Lattice	Polynomial multiplication	$(\mathbb{Z}/q\mathbb{Z})[X]/(X^n + 1)$	q is 16-bit n is 256
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Can we do better?

- Exploit ring properties: Combine Schönhage-Strassen with Kronecker
- Use the roots of unity modulo $X^n + 1$ to construct fast **symbolic** NTTs (as in Nussbaumer)

*Harvey. Faster polynomial multiplication via multipoint Kronecker substitution. J. Sym. Comp. 2009.
 New: **Bos**, Renes and Vredendaal: Polynomial Multiplication with Contemporary Co-Processors: Beyond Kronecker, Schönhage-Strassen & Nussbaumer. USENIX Security Symposium, 2022.

Kronecker	1 x 8192-bit multiplication	4096 x 128-bit multiplications
Harvey*	2 x 4096-bit multiplication	2048 x 128-bit multiplications
Harvey* / New	4 x 2048-bit multiplication	1024 x 128-bit multiplications
New	8 x 1024-bit multiplication	512 x 128-bit multiplications
New	16 x 512-bit multiplication	256 x 128-bit multiplications



RUNNING PQC ON EMBEDDED DEVICES

Key sizes

- Many current embedded devices struggle with RSA-3072 keys
→ PQC is order of magnitude larger

Performance

- Not always as bad as people think.
→ Dilithium verification (secure boot, update) “only” 1x – 3x slower
- Notable disadvantages: variable signing time in Dilithium: probability run-time twice as slow than average is 14 percent
- Possibility to re-use existing hardware to accelerate lattice-based crypto

Memory usage

- Many schemes use a lot of stack by default (50 – 100 KiB).
→ Dedicated techniques needed



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What about high security implementation?

FO-CALYPSE



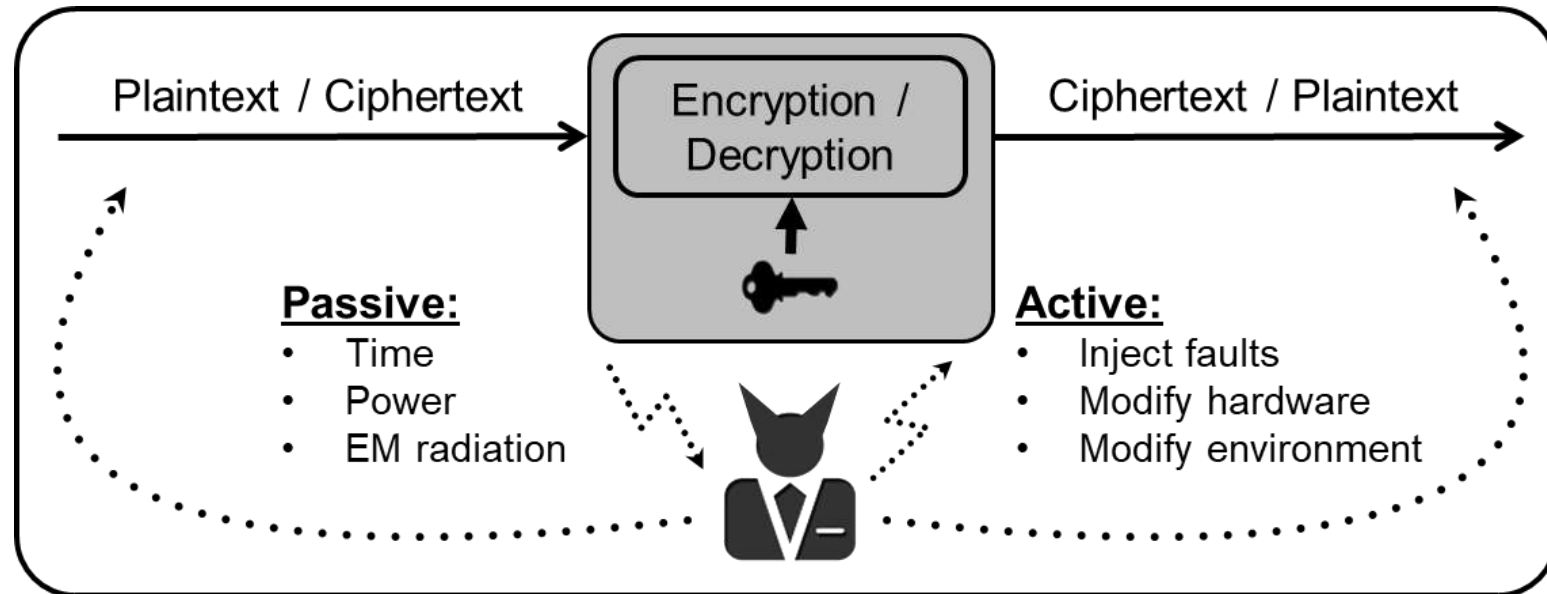
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High-assurance implementations

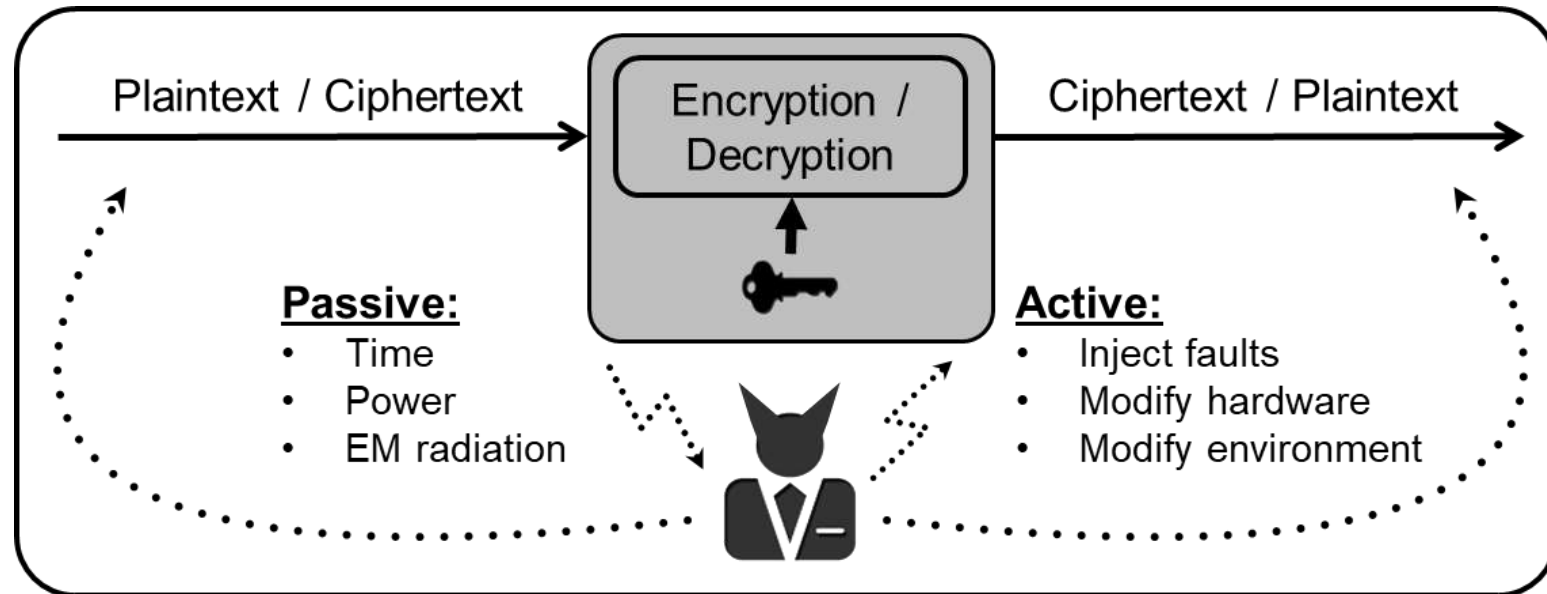


Use meta-information to extract information about the key used in your target platform / product. Many powerful techniques:

fault injections, simple power analysis, differential power analysis, correlation power analysis, template attacks, higher-order correlation attacks, mutual information analysis, linear regression analysis, horizontal analysis, etc



High-assurance implementations

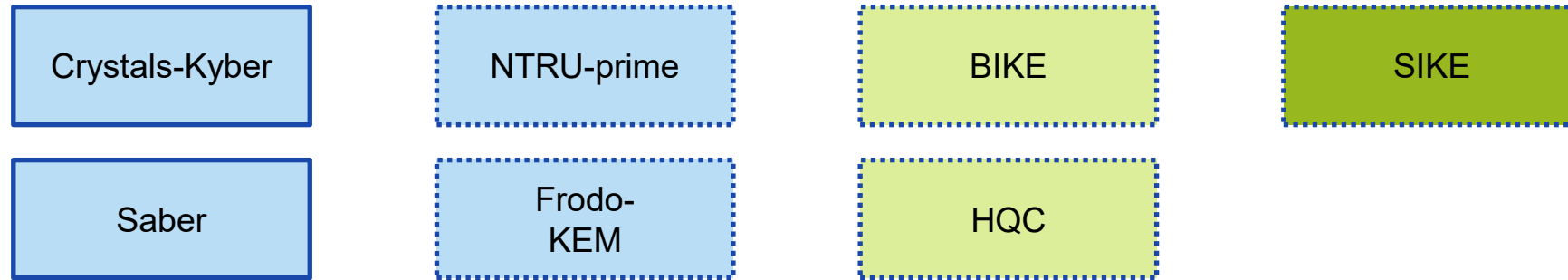


It took many years to find secure and fast protections for RSA + ECC → still cat-and-mouse game

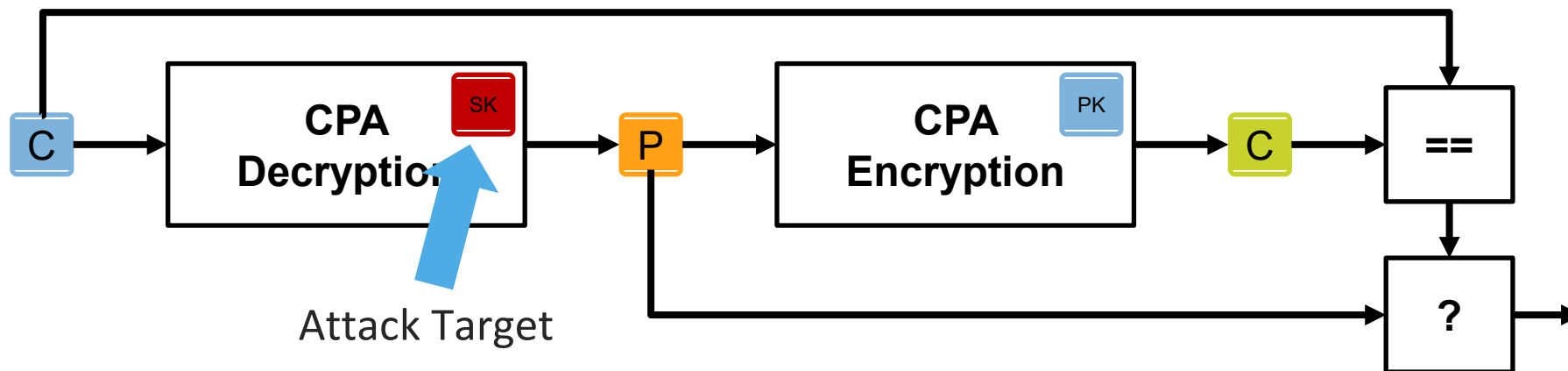
What about Post-Quantum Cryptography?

THE SCA PROBLEM OF THE FO-TRANSFORM

The Fujisaki-Okamoto (FO) transformation (or slight variants) underlies the IND-CCA security of many KEMs, e.g.:



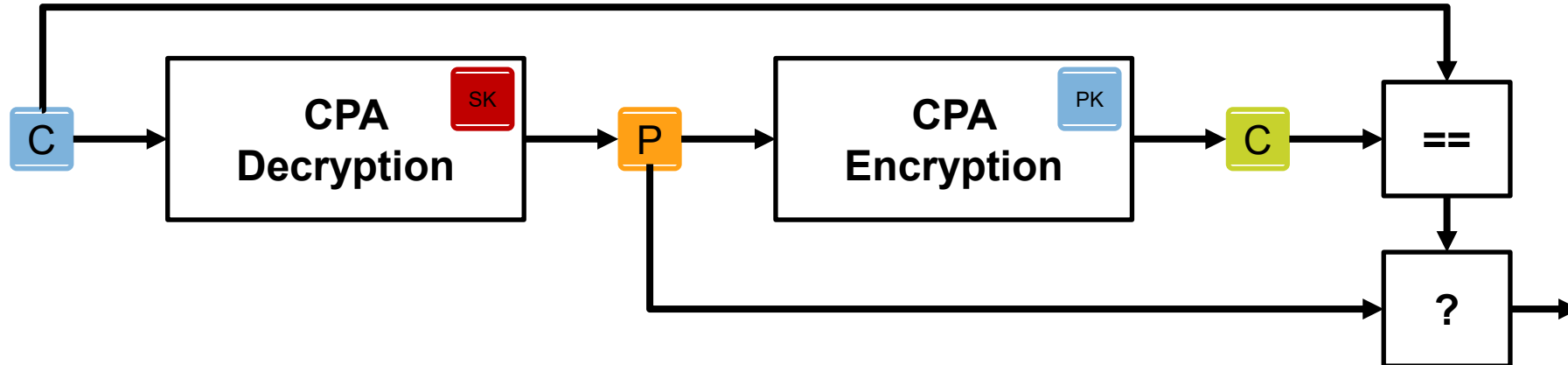
Exemplary Decapsulation:



THE SCA PROBLEM OF THE FO-TTRANSFORM

Attack 1: Chosen Plaintext

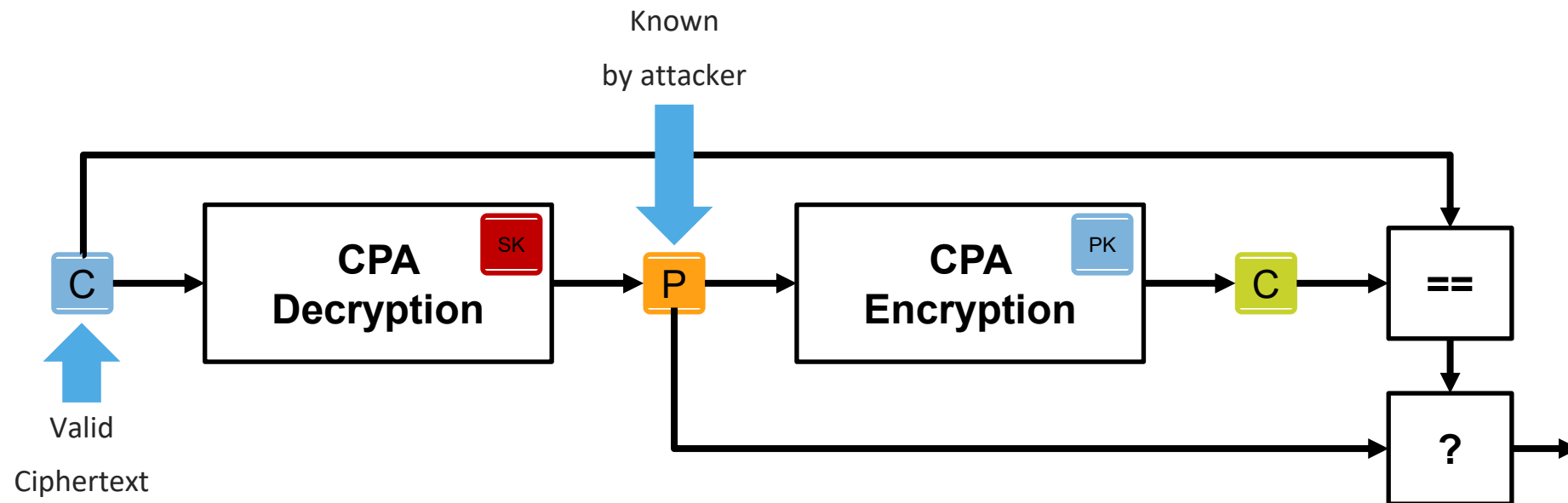
- Attacker inputs only valid ciphertexts



THE SCA PROBLEM OF THE FO-TRANSFORM

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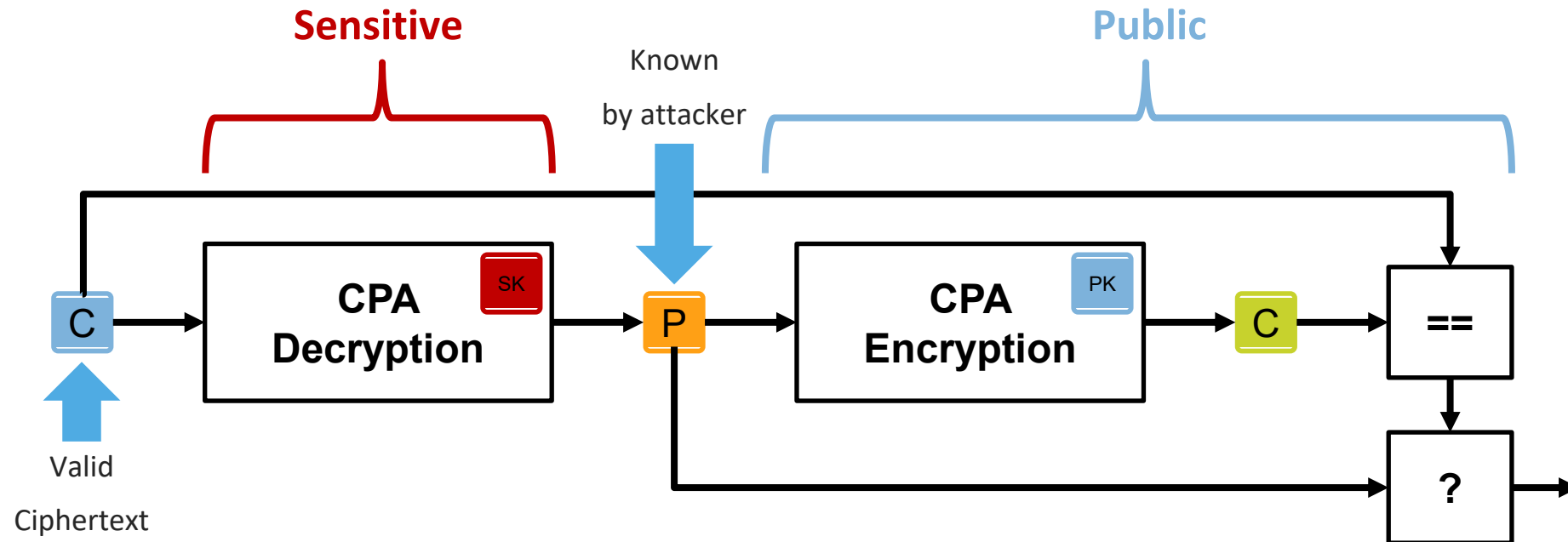
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THE SCA PROBLEM OF THE FO-TTRANSFORM

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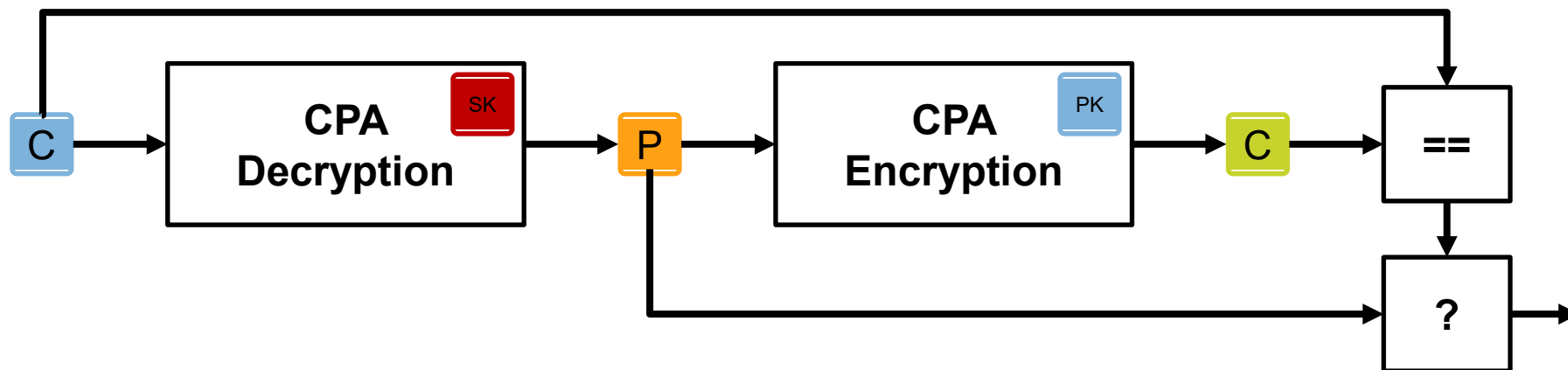
- Attacker inputs only valid ciphertexts
- Attack focuses on **CPA Decryption**, everything after (and including) **P** is public
- Only need to protect **CPA Decryption**



THE SCA PROBLEM OF THE FO-TTRANSFORM

Attack 2: Chosen Ciphertext

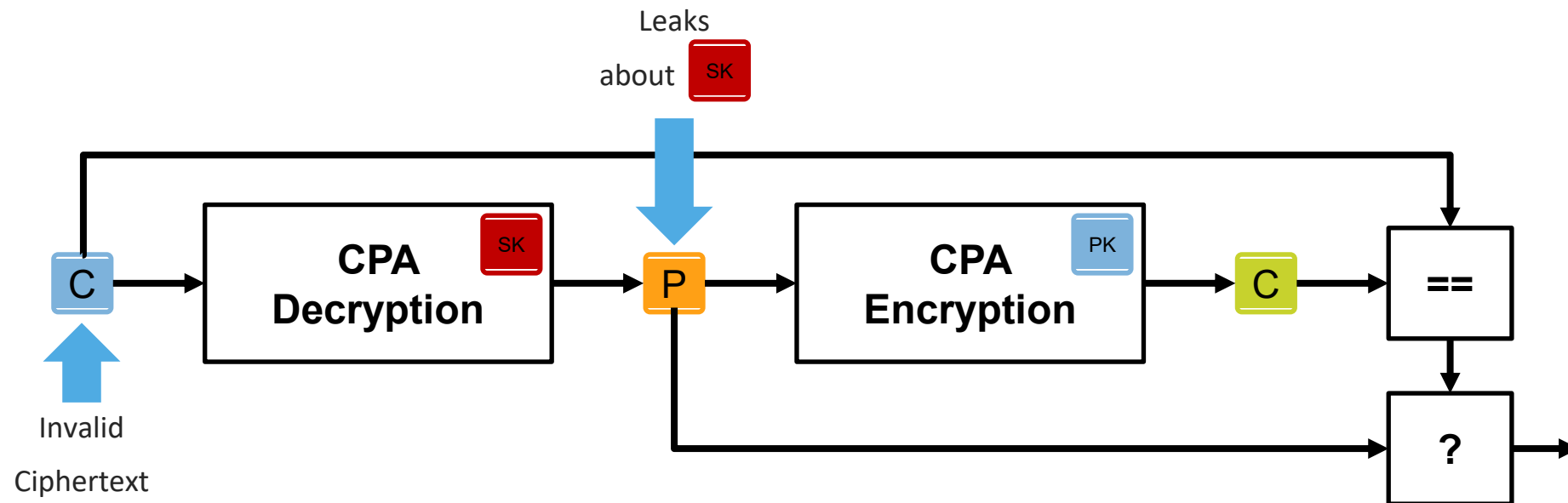
- Attacker inputs specially-crafted invalid ciphertexts



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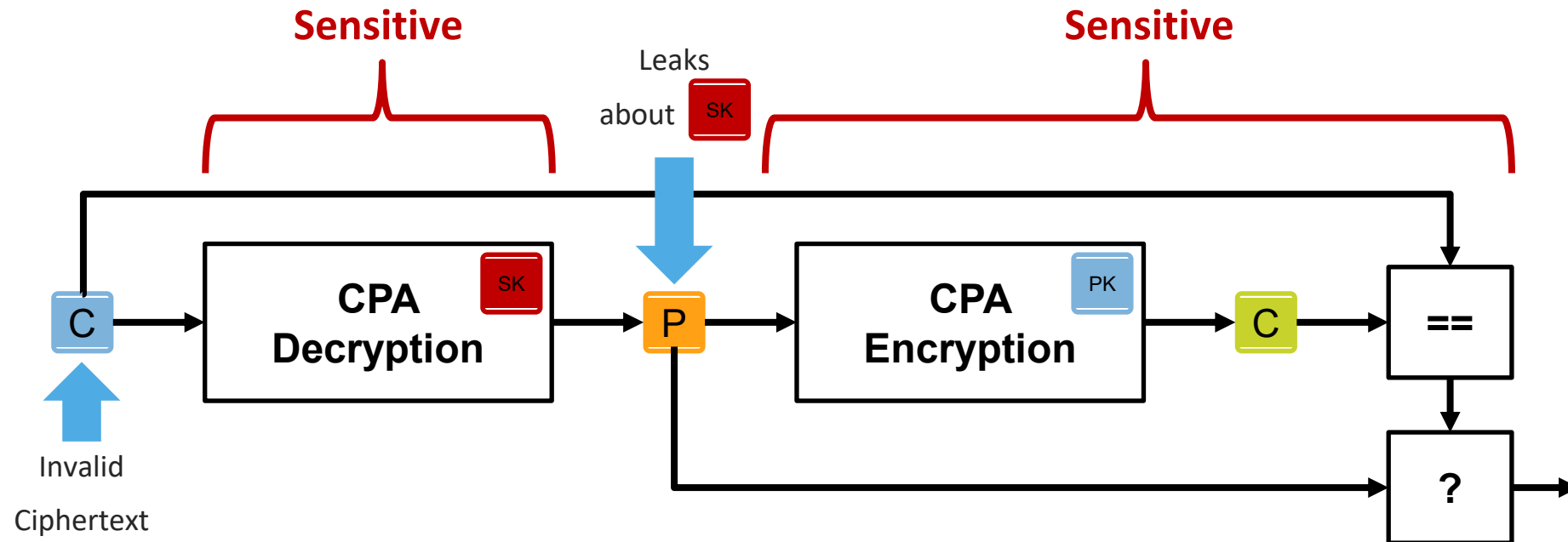
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THE SCA PROBLEM OF THE FO-TTRANSFORM

Attack 2: Chosen Ciphertext

- Attacker inputs specially-crafted invalid ciphertexts
- Attack focuses on **CPA Decryption** + everything after (and including) **P** is potentially sensitive
- Potentially **all (or most) modules** need to be hardened





THE SCA PROBLEM OF THE FO-TRANSFORM



Why is it bad?



Millions of Points of Interest (PoI)

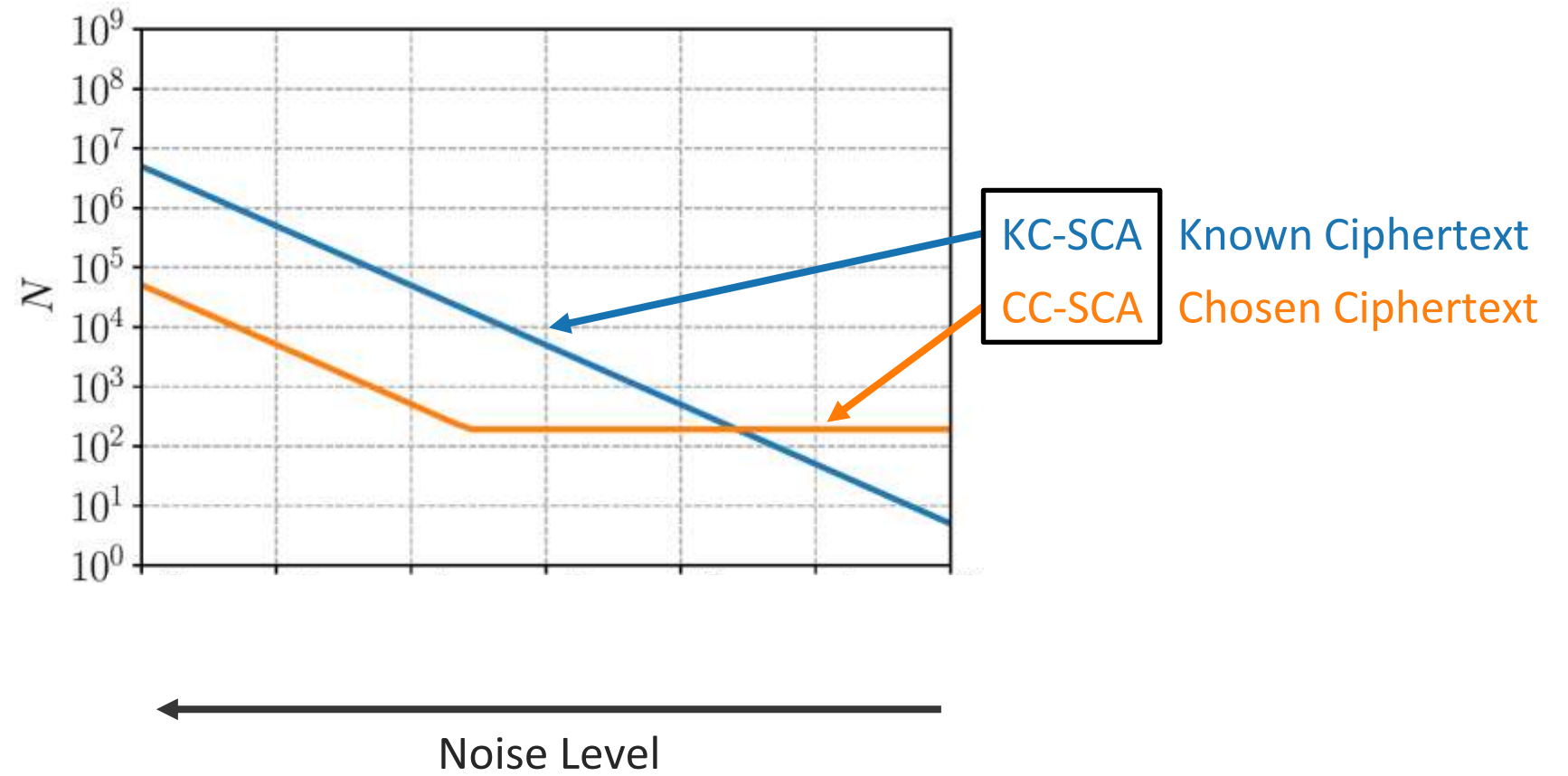
Most recently at TCHES-2022:

Masked Kyber / Saber is broken with only 15k traces.

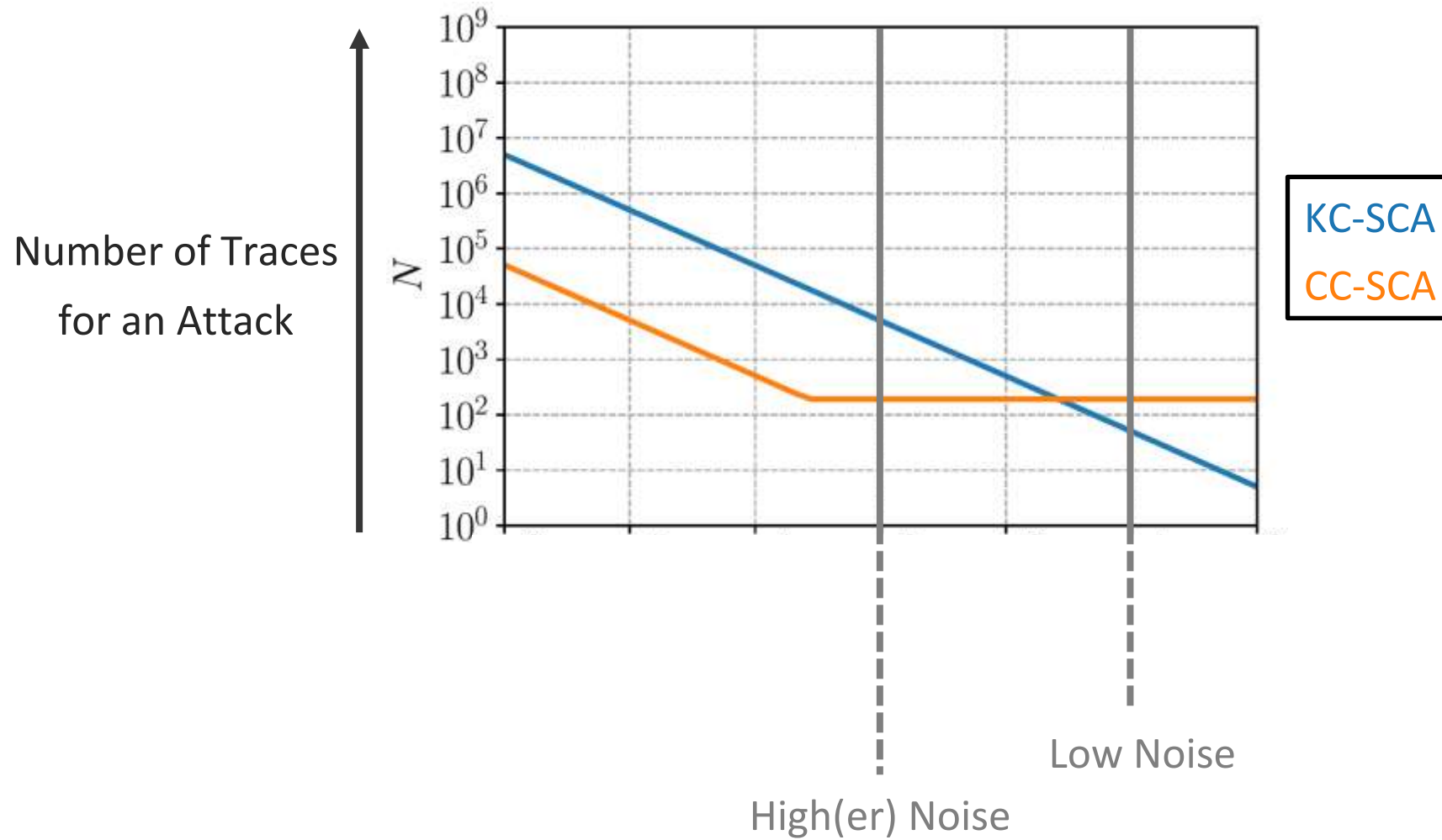
Curse of Re-encryption: A Generic Power/EM Analysis on Post-Quantum KEMs

Rei Ueno^{1,2,3}, Keita Xagawa⁴, Yutaro Tanaka^{1,2}, Akira Ito^{1,2},
Junko Takahashi⁴ and Naofumi Homma^{1,2}

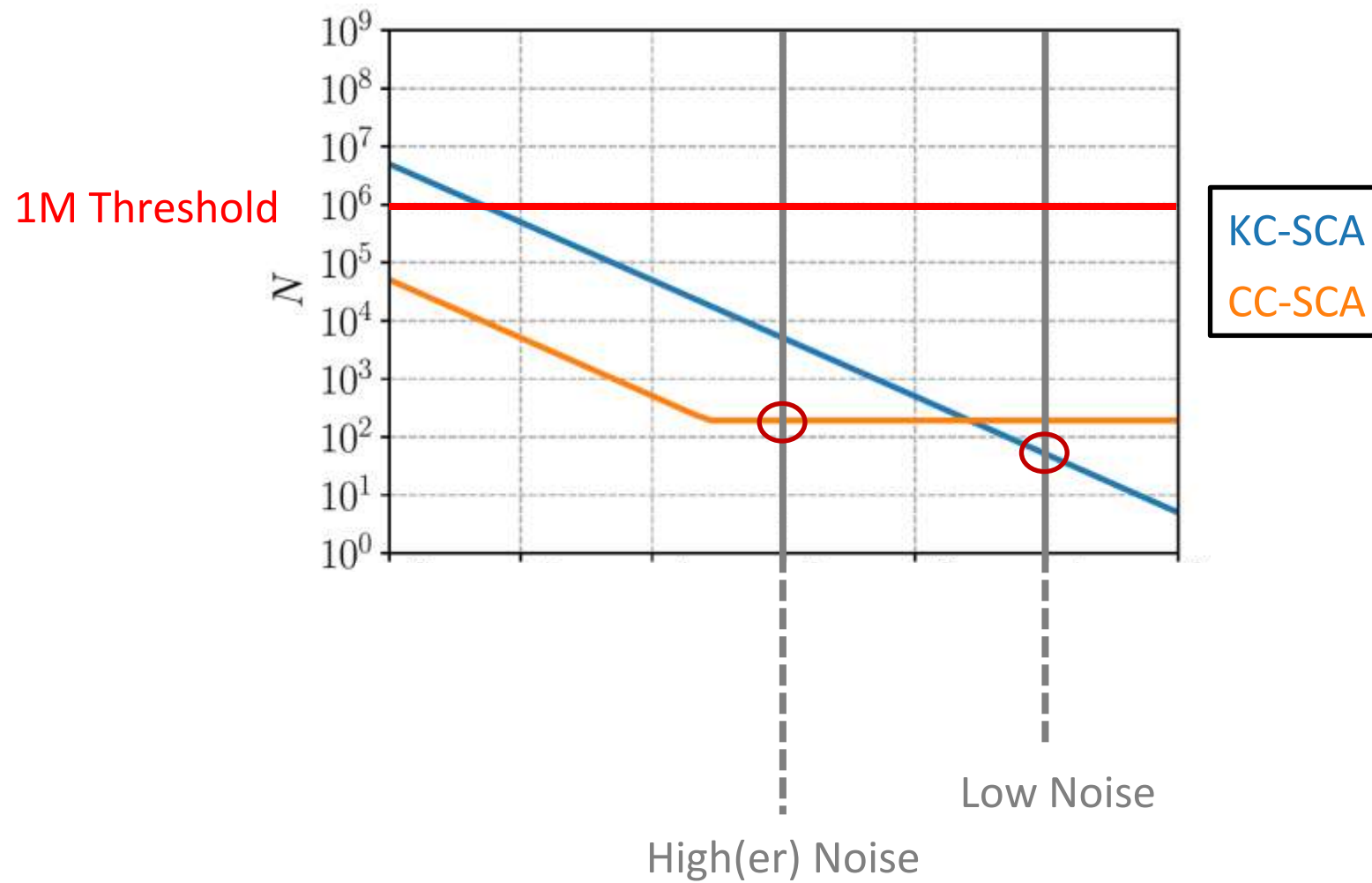
CASE STUDY: UNPROTECTED KYBER



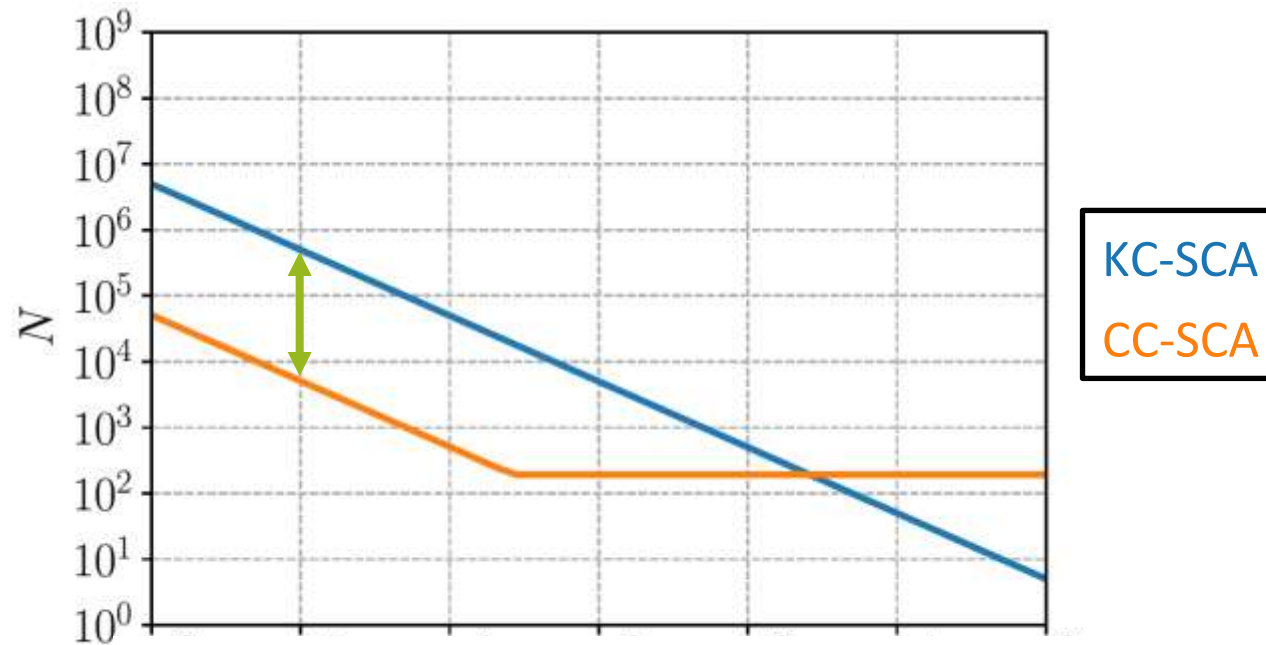
CASE STUDY: UNPROTECTED KYBER



CASE STUDY: UNPROTECTED KYBER



CASE STUDY: UNPROTECTED KYBER



- Unprotected Kyber is (unsurprisingly) not sufficient for both noise levels
- There is a gap of roughly **x100** between the attacks for high(er) noise



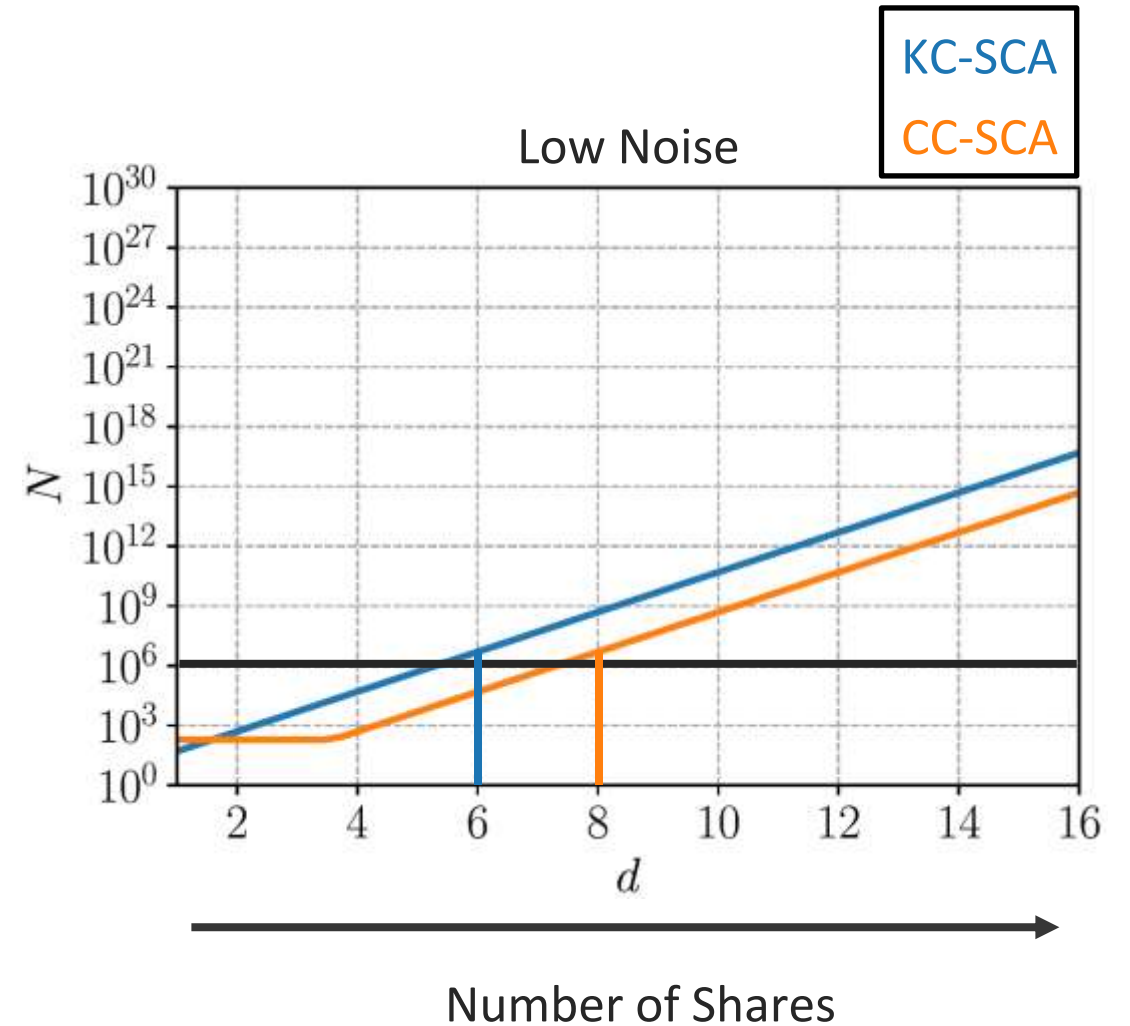
Can this be overcome through masking?

CASE STUDY: MASKED KYBER

Split variables into d shares.

Higher d = Higher security + Increased cost

Pre-Quantum: Certified industrial solutions $d = 2-3$



CASE STUDY: MASKED KYBER

Split variables into d shares.

Higher d = Higher security + Increased cost

Pre-Quantum: Certified industrial solutions $d = 2-3$

For **low noise**:

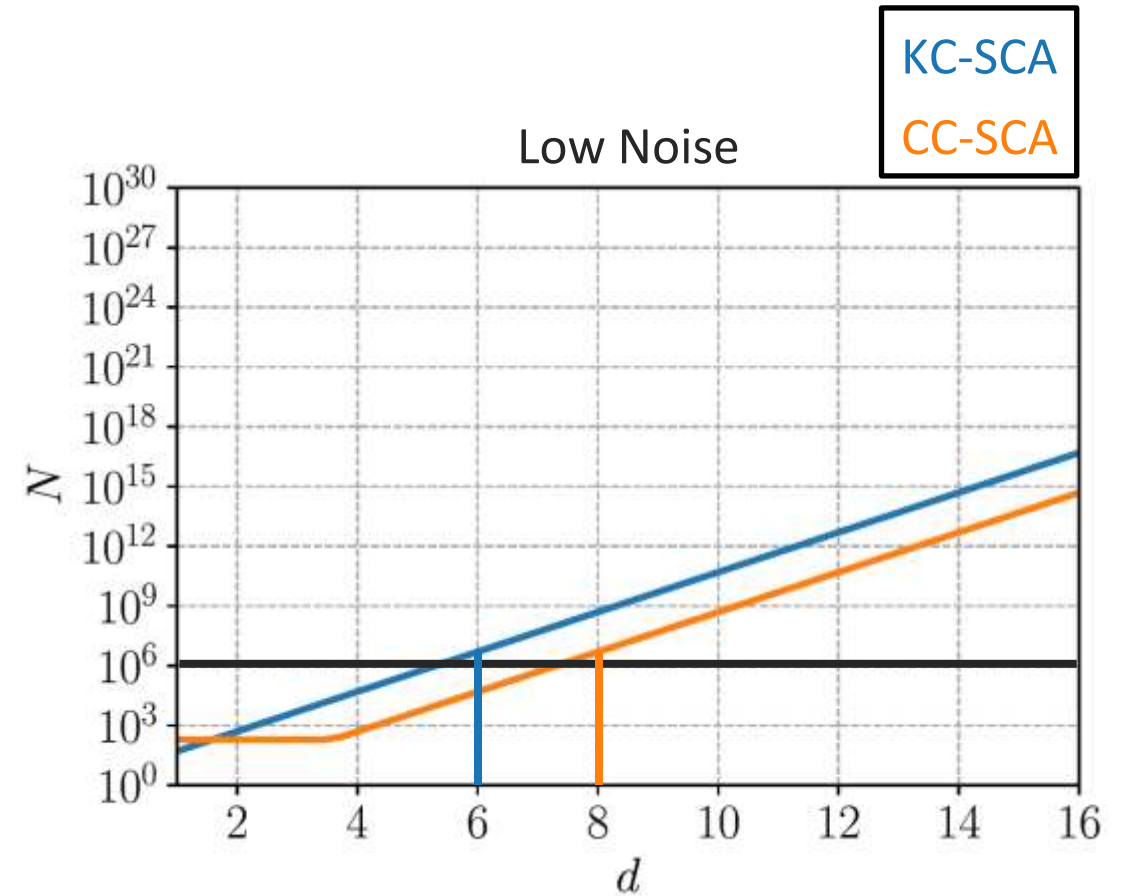
- Known ciphertext → $d = 6$
- Chosen ciphertext → $d = 8$

FO leakage causes an increase of **2** shares.

For **high(er) noise**:

- Known ciphertext → $d = 2$
- Chosen ciphertext → $d = 3$

FO leakage causes an increase of **1** share.





SURVIVAL STRATEGIES

Higher-Order Masking

Case Study: Higher-order masked Kyber (M4) from [BGR+21]
(with adapted A2B)

Overhead compared to unprotected ($d=1$):

d=2	d=3	d=4	d=5	d=6	d=7
3.5x	64x	110x	197x	293x	397x

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└─┬─> High(er)
18x

SURVIVAL STRATEGIES

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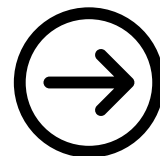
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3.5x	64x	110x	197x	293x	397x	
18x → High(er)					?	

* For this specific implementation + board.

Requires further stack usage optimization.



Leakage caused by the FO significantly increases deployment costs of affected KEMs



SURVIVAL STRATEGIES

Alternative Solution: Encrypt-then-Sign KEM

Replace FO check by **signature verification** for some use cases

- Uses less shares because no FO leakage
- Verification only with public values (no SCA protection)

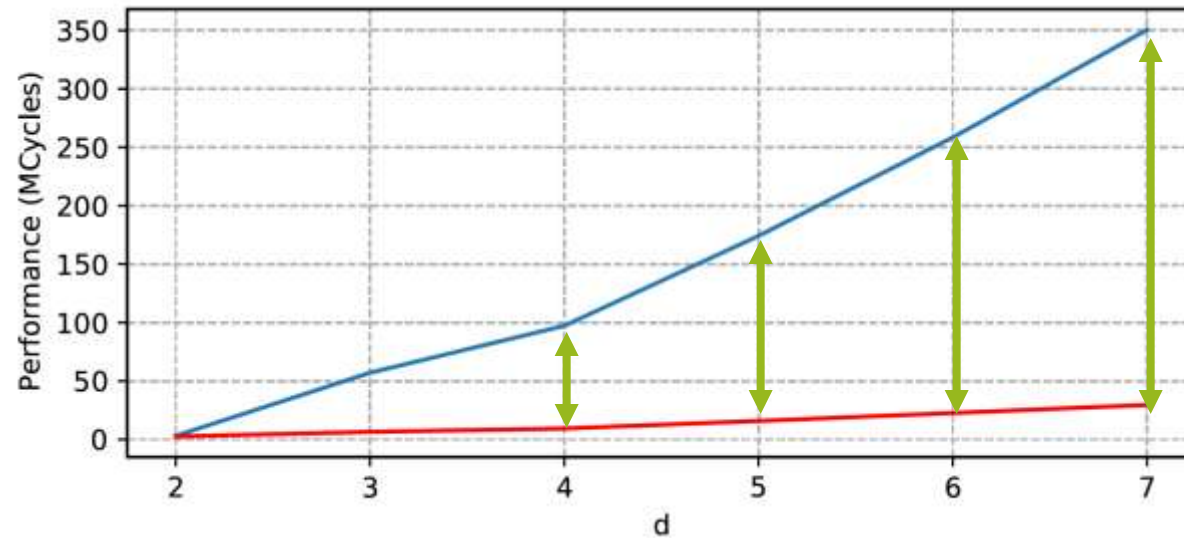
SURVIVAL STRATEGIES

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Example: Kyber + Dilithium



Speed-Up
~10x



CONCLUSIONS

Irrelevant if the quantum threat is real or not

New PQC-Standard are coming!

→ Post-quantum crypto is already being requested

For embedded platforms challenges in terms of

- Performance, memory and key-sizes
- How to efficiently achieve protection against sophisticated side-channel attacks?

✓ **Think about migration paths now**

✓ **Exciting times to work on crypto & security solutions!**

CONTACT: PQC@NXP.COM | [NXP.COM/PQC](https://www.nxp.com/PQC)

THANK YOU.

QUESTIONS?



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