

Gevallenstudies Wiskundige Ingieurstechnieken

Joppe Bos

March 2025





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Cryptographic Researcher and Technical Director at NXP Semiconductors

Secretary of the IACR (2017-2019, 2020-2022)

Editor of the Cryptology ePrint Archive (2019-today)

Editor-in-Chief of the IACR Communications in Cryptology

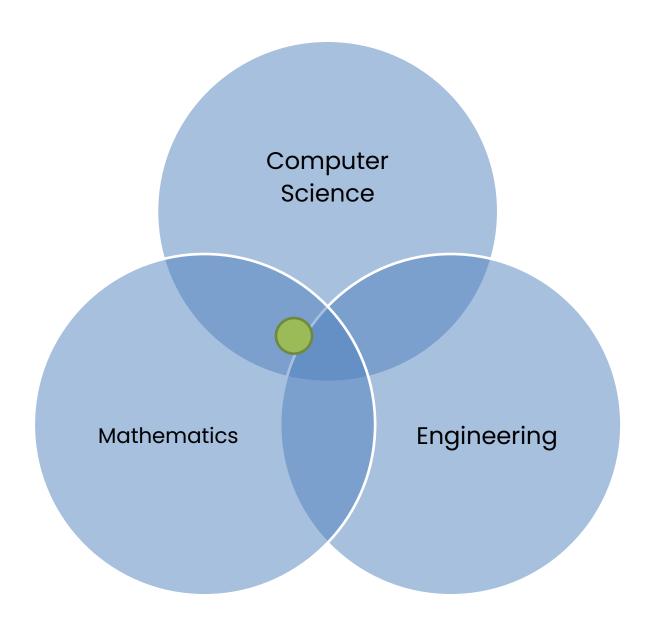
WHOAMI

- Cryptographic researcher + Technical Director
 - in the competence center crypto & security at NXP Semiconductors, Leuven
 - Lead the PQC team
 - Lead security + crypto funded projects & university relations
- Post-doc
 - Cryptography Research Group at Microsoft Research, Redmond, USA.
- PhD in Cryptology
 - EPFL, Lausanne, Switzerland
- Bachelor / Master in Computer Science
 - University of Amsterdam

Public Key Cryptography

Computational number theory

> Number theoretic transform





Breaking ECC

112-bit ECDLP solved using 224 PlayStation 3 game consoles.

NXP Corporate Overview

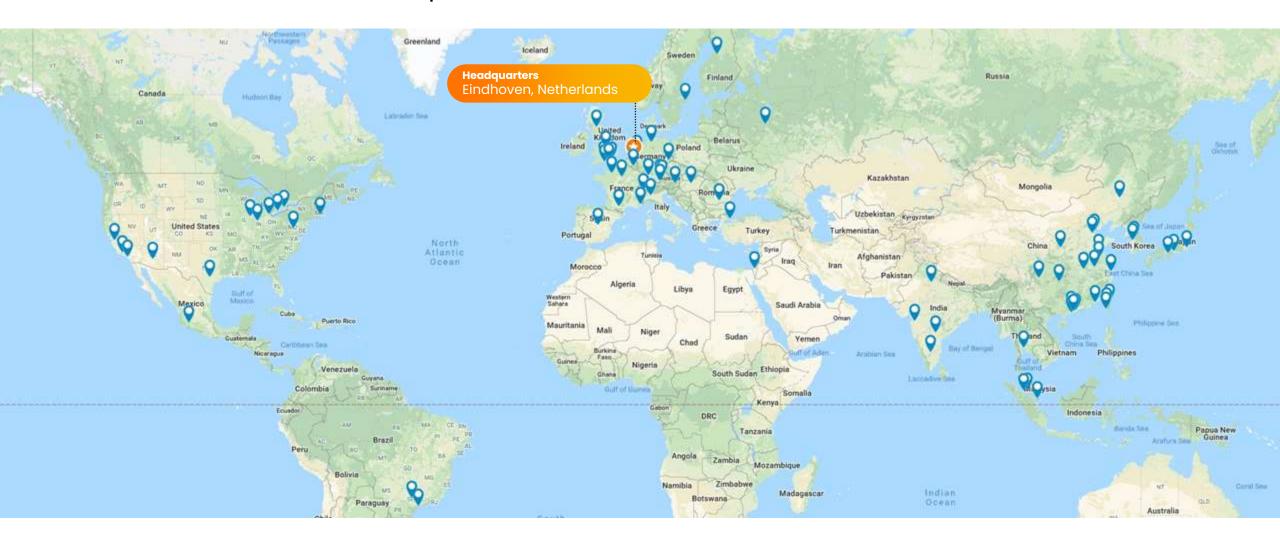
Together we accelerate the breakthroughs that advance our world

We design purpose-built, rigorously tested technologies that enable devices to sense, think, connect and act intelligently to improve people's daily lives.



NXP locations

~34,200 team members with operations in more than 30 countries



Automotive

market positions

Automotive

Technology Leadership



#1 Auto processors

#1 Auto applications processors

#1 Auto RF

#1 Auto DSPs

#1 Cross-domain processors

Applications Leadership

#1 Infotainment

#1 Car radio

#1 Secure car access

#1 In-vehicle networking



Edge processing – a distributed intelligence pyramid

Millions

Cloud

Data centers

10's to 100's Millions

Network Edge Network computing

Billions

Application Edge IoT end points





Edge processing served market

End-to-end solutions for Matter

A unified IP-based protocol to securely and robustly connect smart devices with each other, regardless of brand, and across smart home platforms

Bring interoperability in the Smart Home industry

Simplify development for "things"

Increase reliability for consumers

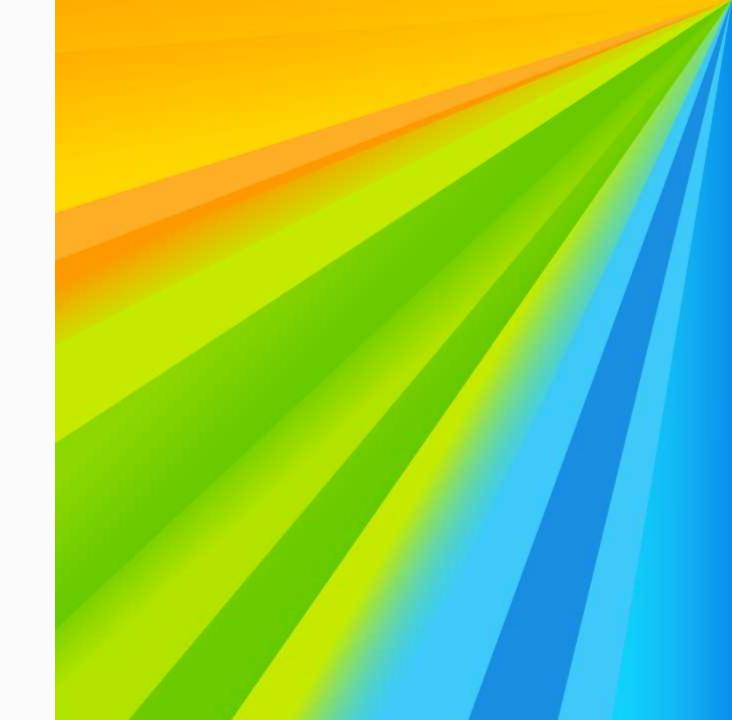
Ensure security and privacy

Led by global brands and 200+ companies





Classical Cryptography



Public-Key Cryptography

In **<u>public-key</u>** cryptography the theoretical foundation of the schemes used are problems which are believed to be hard

- Integer factorization problem (RSA)
- Discrete logarithm problem (DSA, ElGamal)

One of the main ingredients to these problems is a group

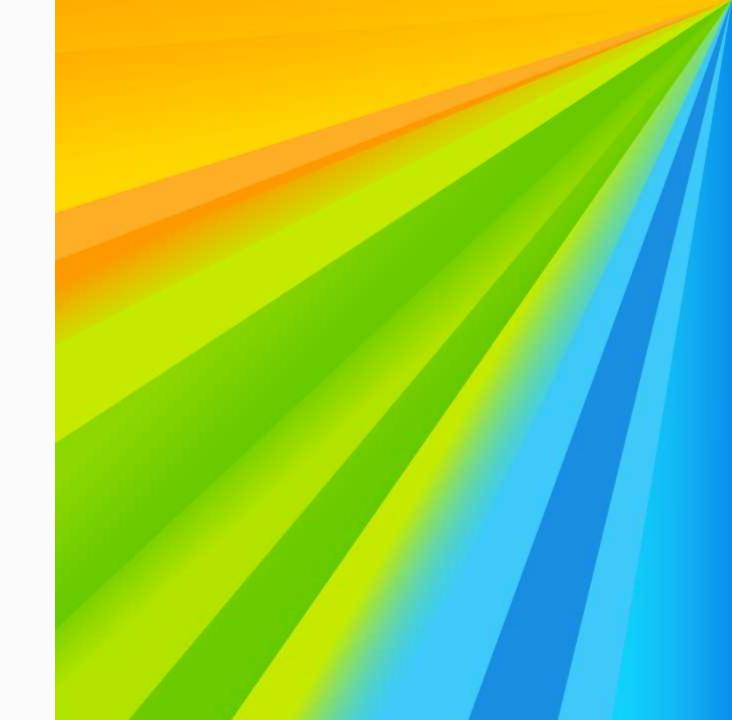
RSA $\rightarrow (\mathbb{Z}/N\mathbb{Z})^{\times} \rightarrow \text{integers } [1,2,...,N-1] \text{ which are co-prime to } N$

DSA/ElGamal $\to \mathbb{F}_p^{\times} = (\mathbb{Z}/p\mathbb{Z})^{\times} \to \text{integers } [1,2,...,p-1] \text{ where } p \text{ is prime}$

Elliptic Curve Cryptography $\to E/\mathbb{F}_p \to \text{point on } E(\mathbb{F}_p)$ where p is prime

Application	 Encryption Scheme, Signature Scheme, Identification Scheme, etc.			
Cryptosystem	DSA, ElGamal, S	Schnorr, etc.	RSA, Rabin, etc.	
Computational Problem	 The Discrete Loga in a Group of p		The Factoring Problem	
Algebraic Structure	 The multiplicative group of integers modulo a prime	Elliptic Curve Group over a Finite Field	The set of integers modulo the product of two primes	

Post-Quantum Cryptography



OUANTUM CLOUD -

How IBM's new five-qubit universal quantum computer works

IBM achieves an important milestone with new quantum computer in the cloud.

Intel Delivers 17-Qubit Superconducting Chip with Advanced Packaging to QuTech



Hello quantum world! Google publishes landmark quantum supremacy claim

The company says that its quantum computer is the first to perform a calculation that would be practically impossible for a classical machine.







May 30, 2024 2:00 PM CEST (UTC+2) by NXP Semiconductors Proc

Eagle's quantum performance progress

Last November, IBM Quantum announced Eagle, a 127-qubit quantum processor based on the transmon superconducting qubit architecture. The IBM Quantum team adapted advanced semiconductor signal delivery and packaging into a technology node to develop superconducting quantum processors.



NXP, eleQtron and ParityQC Reveal their First **Quantum Computing Demonstrator for the DLR Quantum Computing Initiative**

Quantum error correction below the surface code threshold

SHARE

in

 NXP, eleQtron and quantum comput

• It was commissioned by the DLR Quantum Computing Initiative (DLR QCI) to expand the quantum expertise of its partners from research and industry

Google Quantum AI and Collaborators (Dated: August 27, 2024)

Security impact of quantum computers

Requirements: Cryptography Asymmetric Symmetric RSA-3072 AES-128 ECC P-256 SHA-256



"All use of cryptography must use an algorithm that meets at least 128 bits of security."





Quantum potential to destroy security as we know it



Confidential email messages, private documents, and financial transactions

Secure today but could be compromised in the future, even if encrypted



Firmware update mechanisms in vehicles

Could be circumvented and allow dangerous modifications



Critical industrial and public service infrastructure (for healthcare, utilities, and transportation using internet and virtual private networks)

Could become exposed – potentially destabilize cities



Audit trails and digitally signed documents associated with safety (auto certification and pharmaceutical authorizations)

Could be retrospectively modified

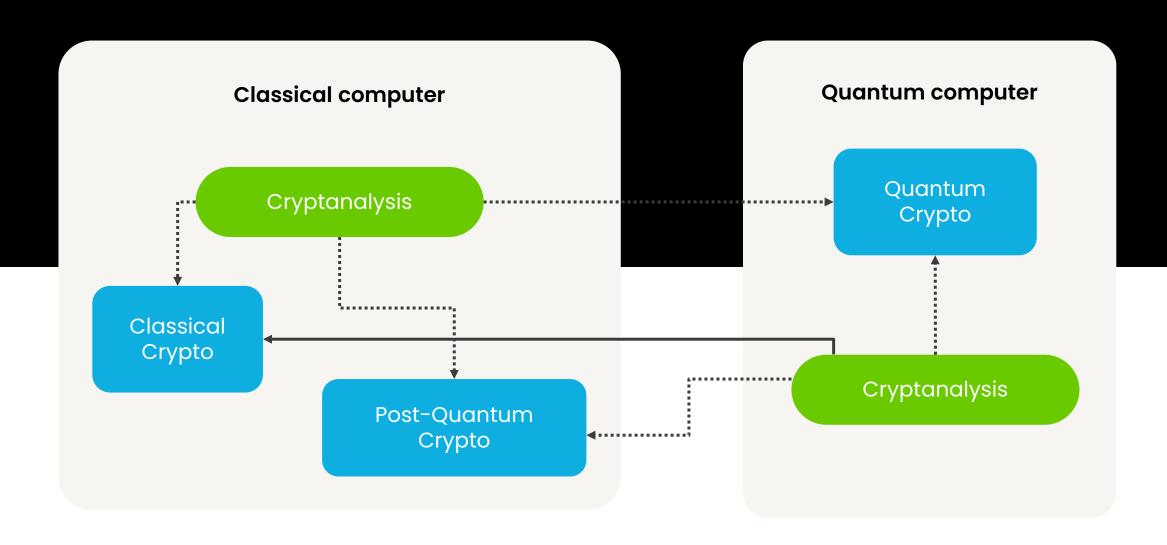


The integrity of blockchains

Could be retrospectively compromised could include fraudulent manipulation of ledger and cryptocurrency transactions



Post-quantum versus quantum crypto





Post-Quantum Cryptography

Requirement 1

Run on classical hardware

Requirement 2

Be secure against adversaries armed with classical computers

Requirement 3

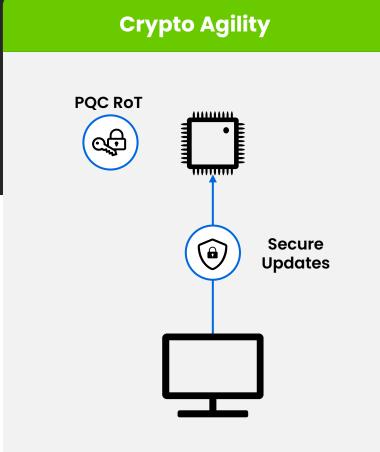
Be secure against adversaries armed with quantum computers

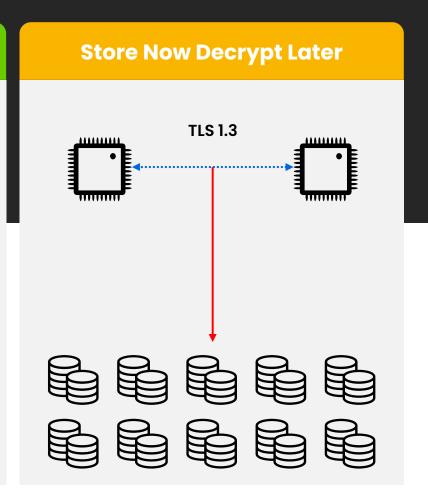
Requirement 4

Be secure against Side-Channel Analysis (SCA) and Fault Injection (FI) attacks

Is Post-Quantum Cryptography relevant for you?



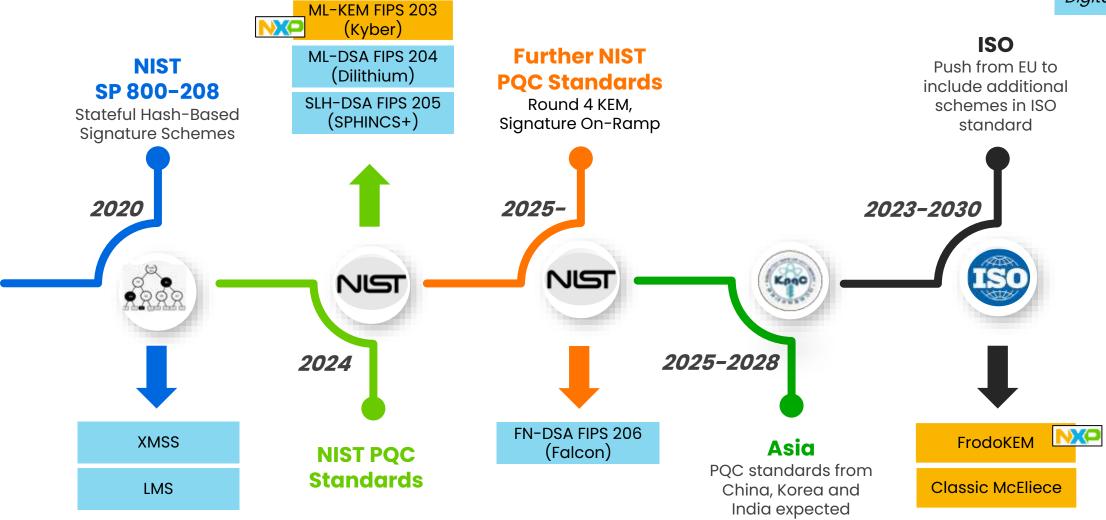




Post-quantum crypto standards are coming It doesn't matter if you believe in quantum computers or not



Digital Signature



PQC Algorithm Standardization

New algorithms and standards



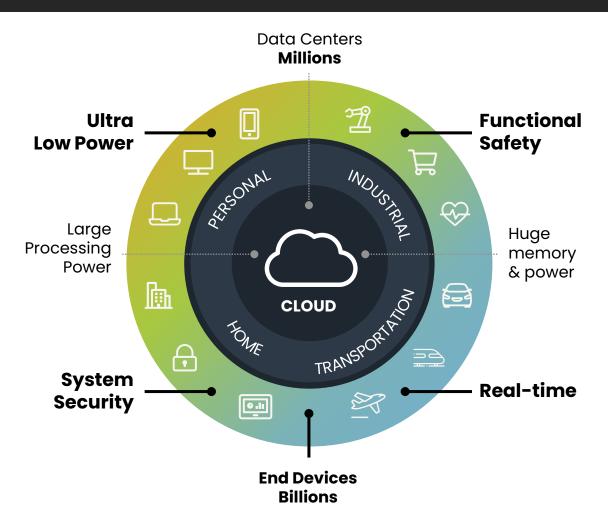




More ongoing and upcoming! FIPS 206, Round 4, On-Ramp, ISO, etc...

- [1] ML-KEM, https://nvlpubs.nist.gov/nistpubs/fips/nist.fips.203.pdf
 [2] ML-DSA, https://nvlpubs.nist.gov/nistpubs/fips/nist.fips.204.pdf
 [3] SLH-DSA, https://nvlpubs.nist.gov/nistpubs/fips/nist.fips.205.pdf
 [4] LMS / XMSS, https://nvlpubs.nist.gov/nistpubs/SpecialPublications/NIST.SP.800-208.pdf

Impact PQC on our eco-system



Data collection, processing and decisions at the edge Devices securely connected to the cloud

No Silver Bullet

If a crypto scheme was better, we would have standardized this already

Cryptographic Keys

Orders of magnitude larger.

In the final: up to 1.3MB

Winners: up to 4.8KB

(ECC: 32 bytes, RSA: 384 bytes)

Performance

Varies: some faster some significantly slower.

SHA-3 is a dominating component (~80%)

Memory

Orders of magnitude more:

up 100KB memory of RAM when executing

NXP has dedicated implementations reaching ~16KB of RAM

Bandwidth & Power

Larger signatures (up to 4.6KB)

- → more bandwidth required
- → increase in power usage

Technical aspects of new algorithms

See pqm4 open source project for benchmarks! [A] Assuming Cortex-M4 @ 200 MHz software-only. For LMS numbers taken from Campos et al. [B]

Algorithm	PQC	Encaps	Decaps	SK	PK	СТ	Algorithm
EC-P384	No	"Fast"	"Fast"	48 B	48 B	96 B	EC-P384
FIPS 203 (ML-KEM)	Yes	4 ms	4 ms	2 400 B	1 184 B	1 088 B	FIPS 203 (ML-KEM)

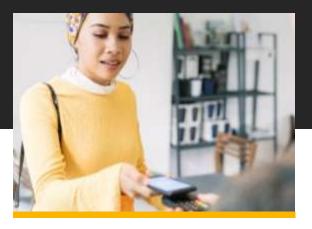
Algorithm	PQC	Encaps	Decaps	SK	PK	СТ	Algorithm
ECDSA-P384	No	"Fast"	"Fast"	48 B	48 B	96 B	ECDSA-P384
FIPS 204 (ML-DSA)	Yes	31 ms	12 ms	4 032 B	1 952 B	3 309 B	FIPS 204 (ML-DSA)
FIPS 205 (SLH-DSA)***	Yes	77 s	68 ms	96 B	48 B	16 224 B	FIPS 205 (SLH-DSA)***
SP 800-20 (LMS/XMSS)	Yes	**(Stateful) 19 s	13 ms	48 B	48 B	1860 B	SP 800-208 (LMS/XMSS)

^{*} NIST Level 3 parameter sets ** Significant reduction possible by increasing memory consumption for state *** New parameter sets coming that will improve performance & signature size!

What is the impact on the billions of embedded devices?









Automotive

Industrial & IoT

Mobile

Communication Infrastructure

70%

70% connected cars by 2025

12B

IoT Edge & end nodes from **6B units** in 2021 to **12B units** in 2025 60B

Tagging **60B products** per year by 2025

40B

Secure anchors & services for **40B processors**



Automotive



eGovernment



Bank cards



Smart mobility (MIFARE) cards



Tags & Authentication



Readers



Mobile

Cryptographic Suite for Algebraic Lattices (CRYSTALS)

The Cryptographic Suite for Algebraic Lattices (CRYSTALS) encompasses

- Kyber, a Key Encapsulation Mechanism (KEM) -> referred to in FIPS 203 as ML-KEM
- **Dilithium**, for Digital Signatures -> referred to in FIPS 204 as **ML-DSA**

Theory: same building blocks

- Module Learning with Errors
- Number-Theoretic Transformations

Many new techniques to deal with!

Kyber uses the 'Fujisaki-Okamoto Transform' to get strong security

Dilithium uses 'Rejection Sampling' as a core component for producing signatures

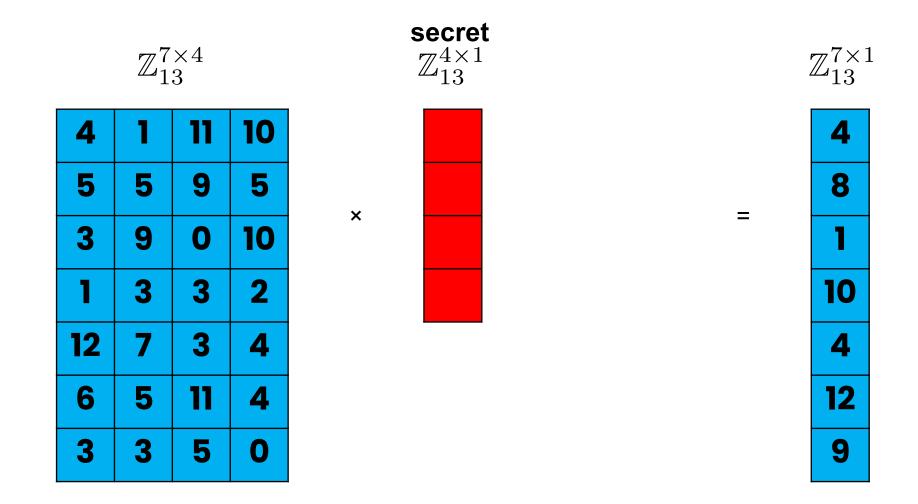






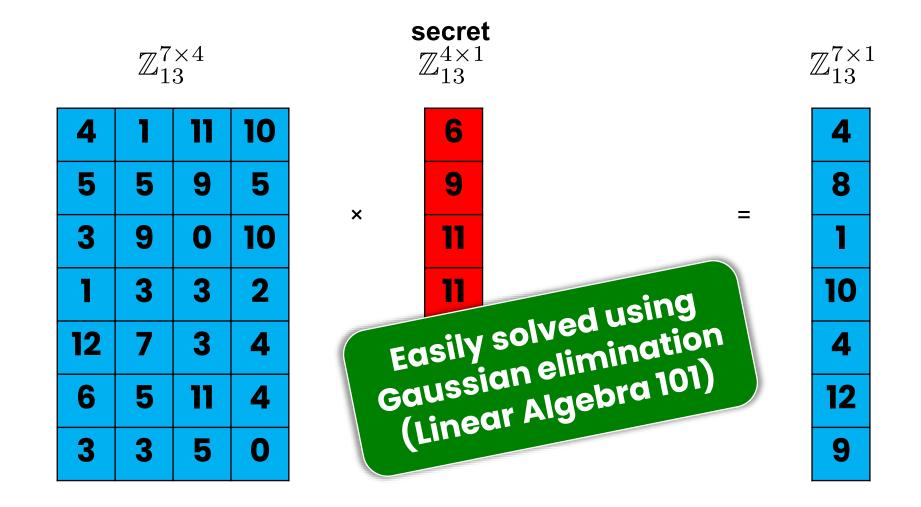


Solving systems of linear equations



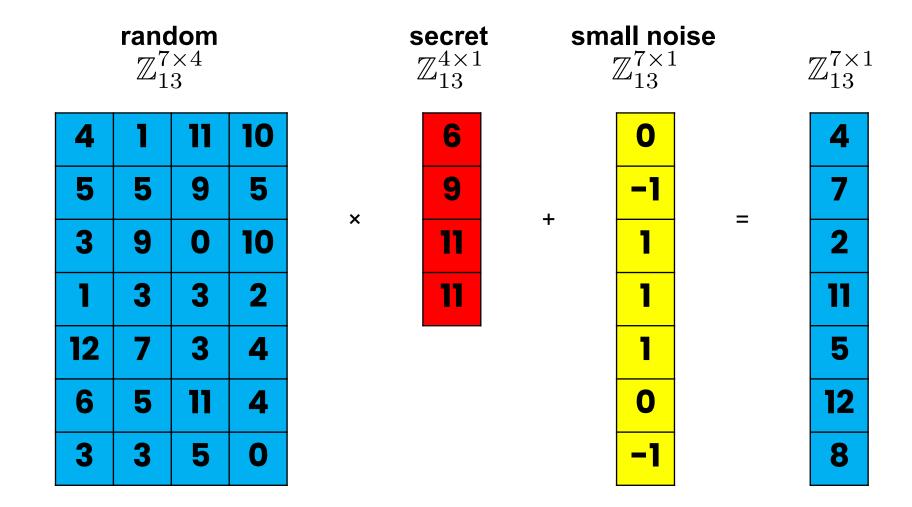
Linear system problem: given blue, find red

Solving systems of linear equations

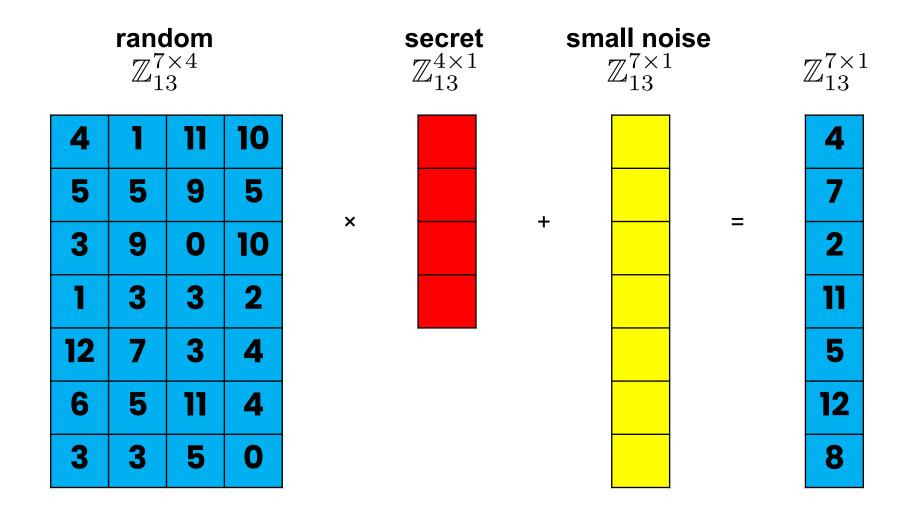


Linear system problem: given blue, find red

Learning with errors problem

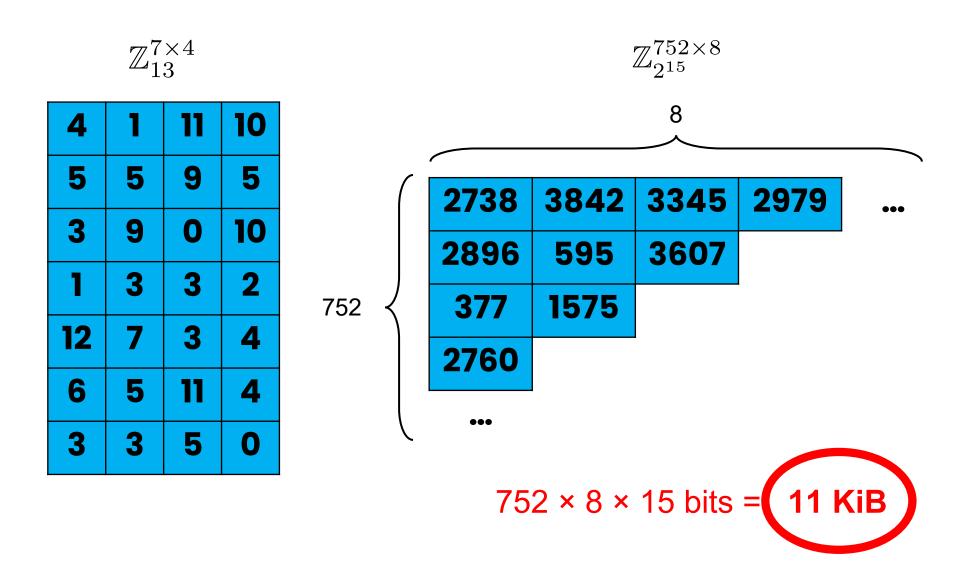


Learning with errors problem



Computational LWE problem: given blue, find red

Toy example versus real-world example



random

$$\mathbb{Z}_{13}^{7 \times 4}$$

4	1	11	10
10	4	1	11
11	10	4	1
1	11	10	4
4	-	11	10
10	4	7	11
11	10	4	1

Each row is the cyclic shift of the row above

random

$$\mathbb{Z}_{13}^{7 \times 4}$$

4	1	11	10
3	4	1	11
2	3	4	1
12	2	3	4
9	12	2	3
10	9	12	2
11	10	တ	12

Each row is the cyclic shift of the row above

. .

with a special wrapping rule: *x* wraps to –*x* mod 13.

random $\mathbb{Z}_{13}^{7\times4}$



Each row is the cyclic shift of the row above

with a special wrapping rule: x wraps to $-x \mod 13$ ($\rightarrow \mathbb{Z}_{13}[x]/\langle x^4+1\rangle$)

So I only need to tell you the first row.

×

$$\mathbb{Z}_{13}[x]/\langle x^4+1\rangle$$

$$4 + 1x + 11x^2 + 10x^3$$

random

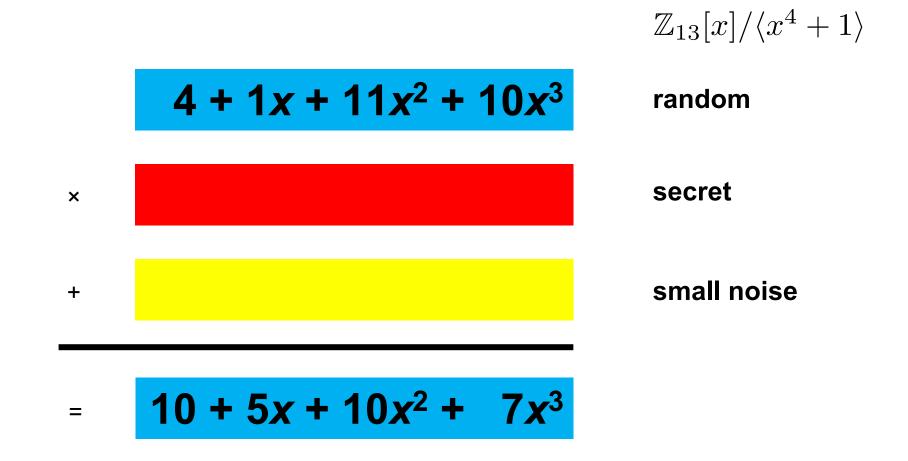
$$6 + 9x + 11x^2 + 11x^3$$

secret

$$+ 0 - 1x + 1x^2 + 1x^3$$

small noise

$$= 10 + 5x + 10x^2 + 7x^3$$



Computational ring-LWE problem: given blue, find red

Basic ring-LWE-DH key agreement

Reformulation of Peikert's ring-LWE KEM (PQCrypto 2014)

public: "big" a in
$$R_q = \mathbf{Z}_q[x]/(x^n+1)$$

Alice

Bob

secret:

random "small" s, e in R_a

secret:

random "small" s', e' in R_a

$$b' = a \cdot s' + e'$$

 $b = a \cdot s + e$

shared secret:

$$s \cdot b' = s \cdot (a \cdot s' \cdot e') \approx s \cdot a \cdot s'$$

shared secret:

$$b \cdot s' \approx s \cdot a \cdot s'$$

These are only approximately equal ⇒ need rounding

What is the impact of PQC on Industrial IoT?



From theory to practice: small-memory implementations

Do these implementations actually run on embedded systems?

		pqm4		
		Runtime	RAM	
Dilithium-2	Sign	19 ms	50 kB	
	Verify	7 ms	11 kB	
Dilithium-3	Sign	31 ms	69 kB	
	Verify	12 ms	10 kB	
Dilithium-5	Sign	42 ms	123 kB	
	Verify	21 ms	12 kB	

From theory to practice: small-memory implementations

Do these implementations actually run on embedded systems?

		pqm4		
		Runtime	RAM	
Dilithium-2	Sign	19 ms	50 kB	
Dilithium-2	Verify	7 ms	11 kB	
Dilithium-3	Sign	31 ms	69 kB	
	Verify	12 ms	10 kB	
Dilithium-5	Sign	42 ms	123 kB	
	Verify	21 ms	12 kB	

NXP PO	QC [A]	Slower	Smaller	
Runtime	RAM	Runtime	RAM	
61 ms	5 kB	3.2x	10.0x	
16 ms	3 kB	2.3x	3.7x	
119 ms	7 kB	3.8x	9.9x	
29 ms	3 kB	2.4x	3.3x	
168 ms	8 kB	4.0x	15.4x	
50 ms	3 kB	2.4x	4.0x	



All Dilithium parameter sets will fit on a device with ~8KB memory.



Price: factor 3 to 4 in performance HW accelerators

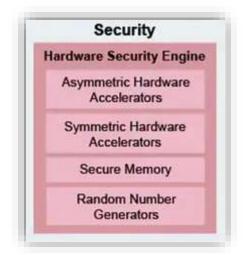


Example of what we do at NXP

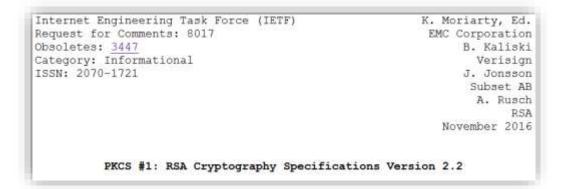
Joppe W. Bos, Joost Renes and Christine van Vredendaal: <u>Polynomial</u> <u>Multiplication with Contemporary Co-Processors: Beyond Kronecker,</u> <u>Schönhage-Strassen & Nussbaumer</u>. <u>USENIX Security Symposium</u> 2022.

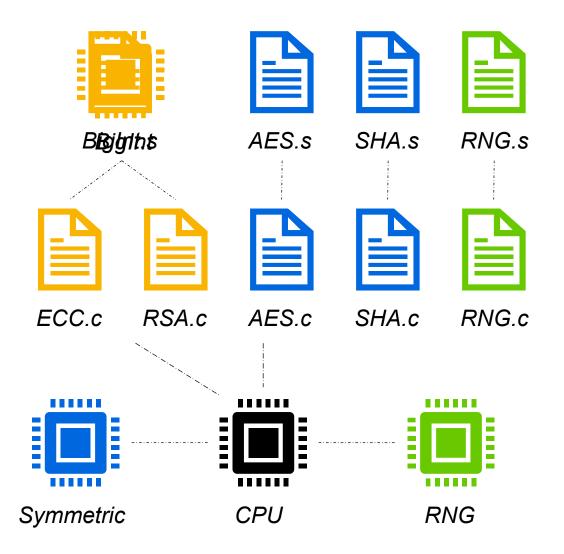
Implementing Classical cryptography





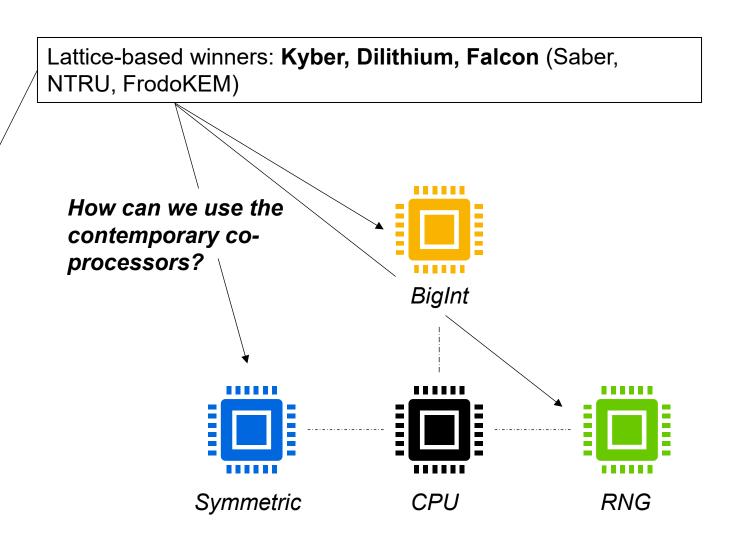
S32G2 automotive processor spec





Implementing post-quantum cryptography





Re-using existing HW

Approac h	Core	Structure	Size	
RSA	Modular multiplication	$(\mathbb{Z}/n\mathbb{Z})^*$	<i>n</i> is 3072-bit	Co-pro present in chip
ECC	Elliptic curve scalar multiplication	$\mathrm{E}(\mathbb{F}_p)$	p is 256-bit	
Lattice	Polynomial multiplication	$(\mathbb{Z}/q\mathbb{Z})[X]/(X^n+1)$	q is 16-bit n is 256	0 0 0
		(Can we use	this?

Kronecker substitution

Polynomial domain

$$f = 1 + 2x + 3x^2 + 4x^3$$

$$g = 5 + 6x + 7x^2 + 8x^3$$

Grundzüge einer arithmetischen Theorie der algebraischen Grössen.

(Von L. Kronecker.)

(Abdruck einer Festschrift zu Herrn E. E. Kummers Doctor-Jubiläum, 10. September 1881.)



$$fg = 5 + 16x + 34x^2 + 60x^3 + 61x^4 + 52x^5 + 32x^6$$

Kronecker domain (with evaluation point 100)

$$f(100) = 4030201$$

$$g(100) = 8070605$$



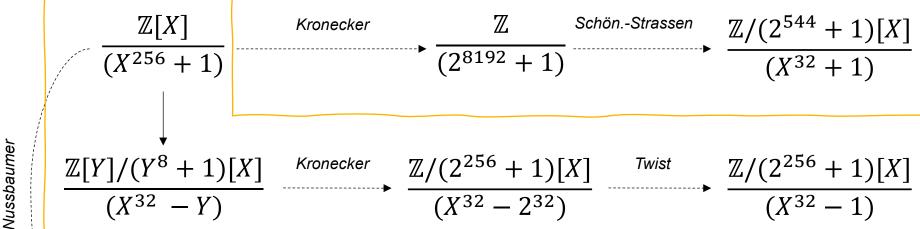
$$fg(100) = 32526160341605$$



Polynomial multiplication techniques

Kronecker evaluation at 2³² Multiplication with a 256-bit multiplier





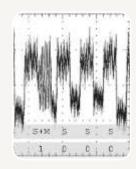
$$\frac{\mathbb{Z}[Y]/(Y^8+1)[X]}{(X^{32}-Y)} \xrightarrow{Kronecker} \frac{\mathbb{Z}/(2^{256}+1)[X]}{(X^{32}-2^{32})} \xrightarrow{Twist} \frac{\mathbb{Z}/(2^{256}+1)[X]}{(X^{32}-1)}$$

Kronecker+

$\mathbb{Z}[Y]/(Y^8+1)[X]$	Kronecker	$\mathbb{Z}/(2^{256}+1)[X]$
$(X^{64}-1)$	•	$(X^{64}-1)$

Algorithm	# Muls	# Bits
Kron. + Schoolbook	1024	256
Kron. + Karatsuba	243	256
Kron. + Toom-Cook	63	256
Kron. + SchönStrassen	32	544
Nussbaumer + Kron.	64	256
Kronecker+	32	256

[[]B] Harvey. Faster polynomial multiplication via multipoint Kronecker substitution. J. of Sym. Comp. 2009.



Side-channel attacks

- Power analysis (SPA, DPA)
- Electromagnetic analysis (SEMA, DEMA)
- Timing Analysis
- Photo-emission microscopy (high-end)
- Profiled, unprofiled and ML-assisted variants

Resistance against physical & logical attacks



Fault injection attacks

- Voltage or clock glitching
- Electromagnetic fault injection (EMFI)
- Body bias injection
- Laser fault injection
- Single and multi-shot scenarios



Invasive attack

- Focused Ion Beam (FIB) modifications
- Micro/Nano-probing of internal signals
- Signal forcing
- Delayering
- · Reverse-engineering

Embedded cryptography and implementation attacks

Attacks

Deep understanding in both academia and industry.



Classic Cryptography

AES 3DES DSA... ECDSA RSA ECC



/₁\

Countermeasures

Practically secure and certified implementations.

Embedded cryptography and implementation attacks

Attacks

Deep understanding in both academia and industry.



Classic Cryptography

AES 3DES DSA... ECDSA RSA ECC



Countermeasures

Practically secure and certified implementations.

Post-Quantum Cryptography

Active research area resulting in increasingly powerful attacks.



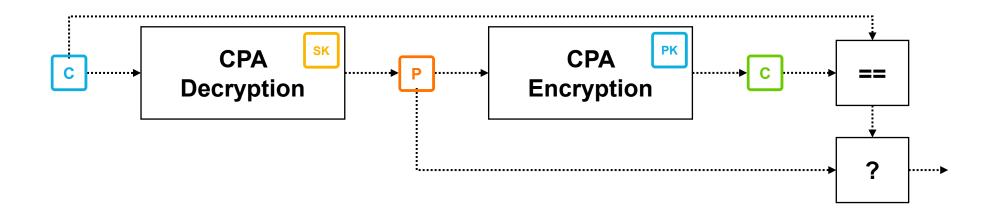
Kyber Dilithium ... SPHINCS+ XMSS





Early stage of academic research.
Limited industrial results.

Fujisaki Okamoto transform



Transform a scheme which achieves IND-CPA ("chosen plaintext attack") security to reach IND-CCA ("indistinguishability against chosen-ciphertext attacks") security

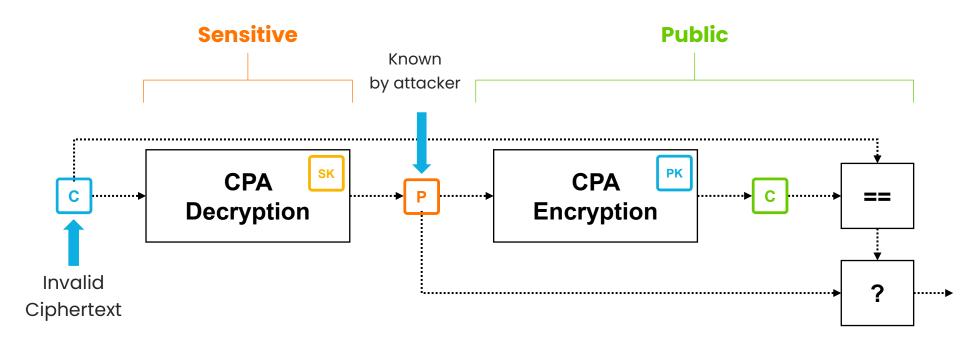
Fujisaki, E. and Okamoto T., Secure integration of asymmetric and symmetric encryption schemes, CRYPTO 1999 and JoC 2013

The SCA Problem of the FO-Transform



Attack 1: Chosen Plaintext

- Attacker inputs only valid ciphertexts
- Attack focuses on **CPA Decryption**, everything after (and including)
- Only need to protect **CPA Decryption**



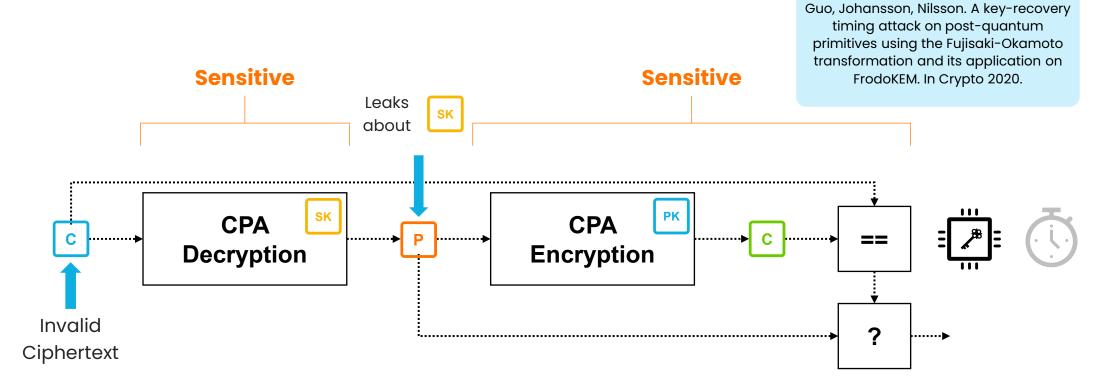
The SCA Problem of the FO-Transform



Attack 2: Chosen Ciphertext

- Attacker inputs specially-crafted invalid ciphertexts
- Attack focuses on **CPA Decryption** + everything after (and including)
- is potentially sensitive

Potentially all (or most) modules need to be hardened



From Theory to practice: Secure implementations (NXP PQC Team)

Only with carefully managed maximum number of issued signatures

First completely masked implementation of Kyber / FIPS 203!

Year	Venue	FIPS 203	FIPS 204	Title		
2021	TCHES			Masking Kyber: First- and Higher-Order Implementations		
2021	RWC			Post-Quantum Crypto: The Embedded Challenge		
2022	TCHES			Post-Quantum Authenticated Encryption against Chosen-Ciphertext SCA		
2022	RWC			Surviving the FO-calypse: Securing PQC Implementations in Practice		
2023	TCHES			From MLWE to RLWE: A Differential Fault Attack on Randomized & Deterministic Dilithium		
2023	TCHES			Protecting Dilithium Against Leakage Revisited Sensitivity Analysis		
2024	RWC			Lessons Learning from Protecting CRYSTALS-Dilithium		
2024	TCHES			Exploiting Small-Norm Polynomial Multiplication with Physical Attacks		
2024	RWC			Challenges of Migration to PQ Secure Embedded Systems		

Completely masked implementation of Dilithium / FIPS 204!

54 | NXP | Public

NXP S32G2 vehicle network processor with PQC integration

Our target platform: \$32G274A

- 3 Lockstep Arm® Cortex®-M7 Microcontrollers
- 4 Cluster Lockstep Cortex-A53 Microprocessors
- 8 MB of System RAM
- Network Accelerators (LLCE/PFE)
- Hardware Security Engine (HSE)
- ASIL D Functional Safety Support



Post-Quantum Crypto

- Integrate PQC secure signature verification
- Protection against Fault Attacks
- Enable PQC secure boot
- · Secure Over-the-Air (OTA) updates
- · Secure vehicle and driver data

www.nxp.com/S32G2





Benchmarks for authentication of FW signature on the S32G2

Alg.	Size		Performance (ms)			
			1 KB		128 KB	
	PK	Sig.	Inst.	Boot	Inst.	Boot
RSA 4K	512	512	2.6	0.0	2.7	0.2
ECDSA-p256	64	64	6.2	0.0	6.4	0.2
Dilithium-3	1952	3293	16.7	0.0	16.9	0.2



Demonstrator only, further optimizations are possible (such as hardware accelerated SHA-3)



Signature verification only required once for installation!



During boot the signature verification can be replaced with a check of the Reference Proof of Authenticity



Conclusions

- We are always looking for talented people in math / crypto!
- Need to have an applied interest as well.
- New mathematical techniques to map algorithms to resource constrained devices.
- Software / hardware skills are a plus
- Crypto / number theory knowledge is a must!

Experience shows it is easier to teach software development skills to an applied mathematician than number theory to an engineer ©

Interested? Job? Internship? Industry PhD with KU Leuven? Contact me: joppe.bos@nxp.com







Get in touch!

Joppe W. Bos

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Brighter Together